



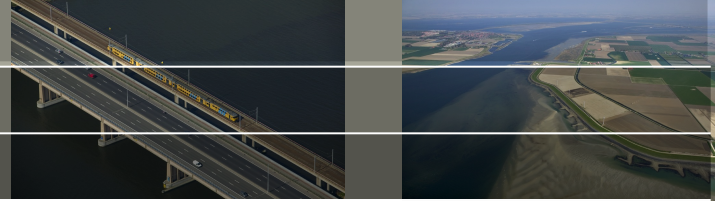
# Modellering van getij op de Noordzee vertikale referentie

Martin Verlaan,  
Firmijn Zijl,  
Julius Sumihar  
Cornelis Slobbe

6 Feb 2014 NCG

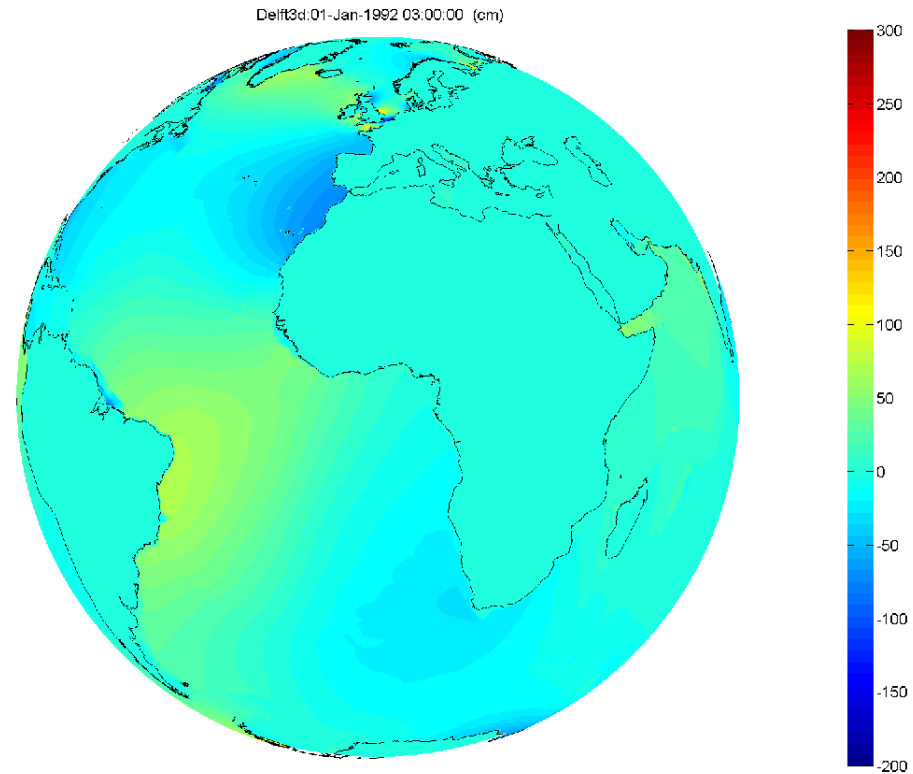
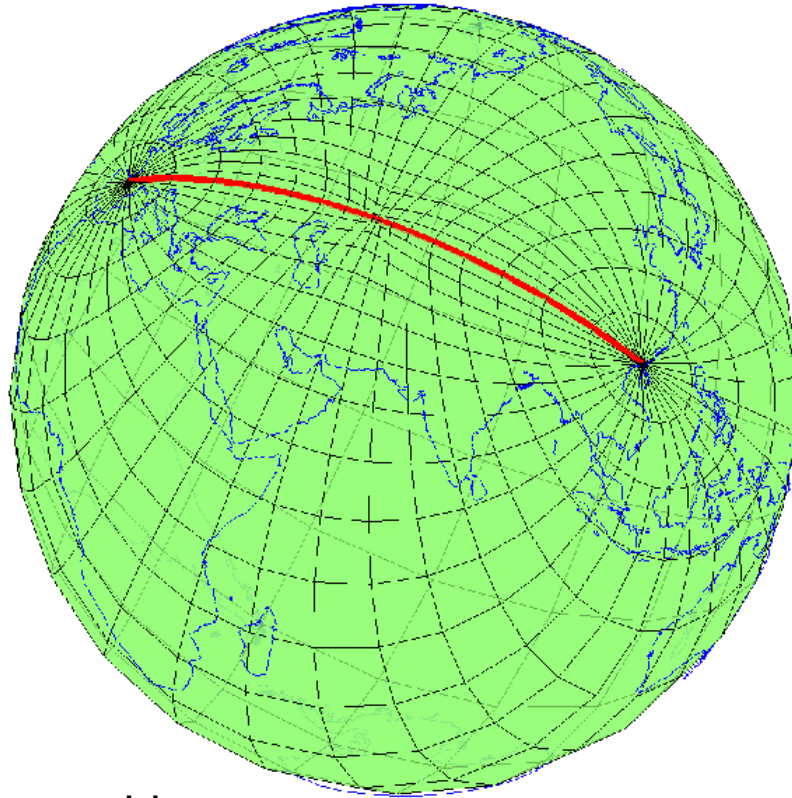
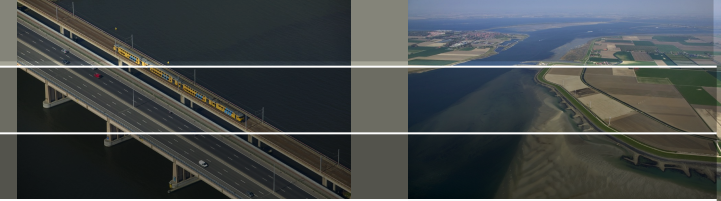


# Outline



- Introduction
  - Observations & harmonic analysis
  - Numerical models
  - Reference surfaces
- MDT and LAT
- More accurate model DCsMv6
- Challenges & future work

# Global tide model



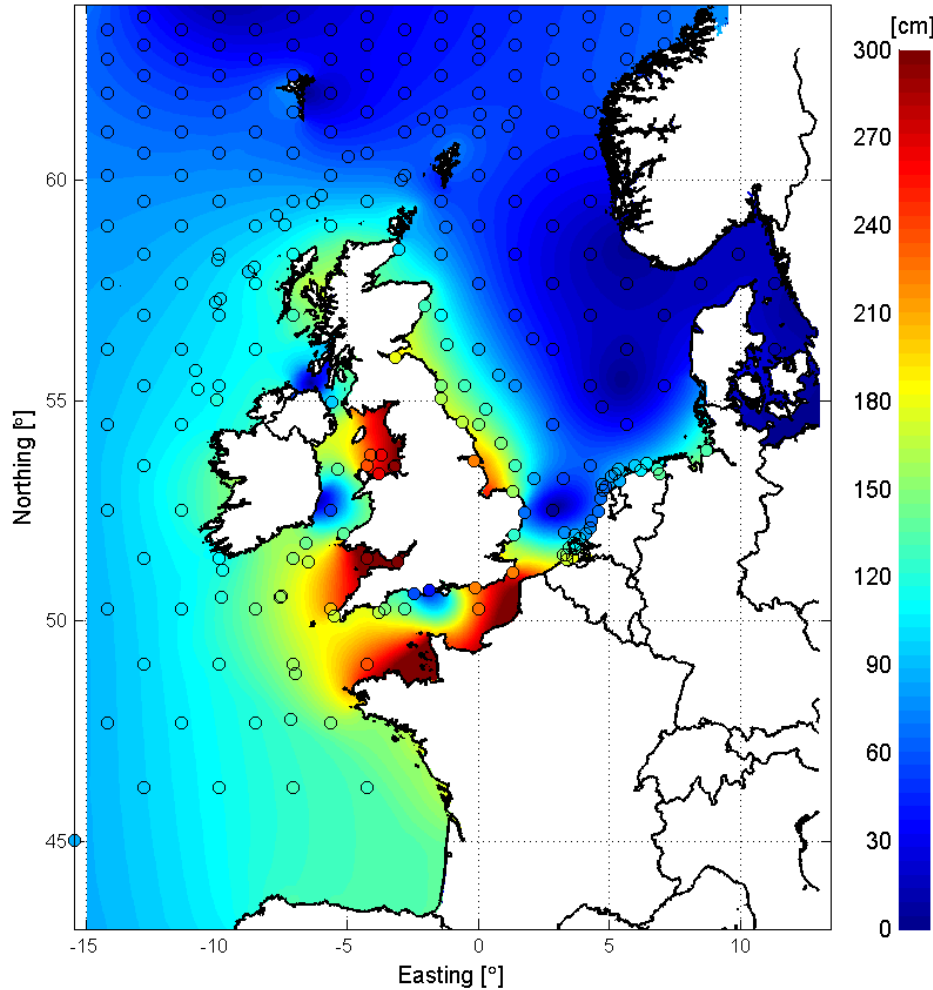
ocean tides



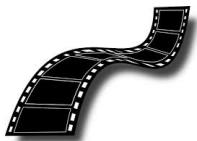
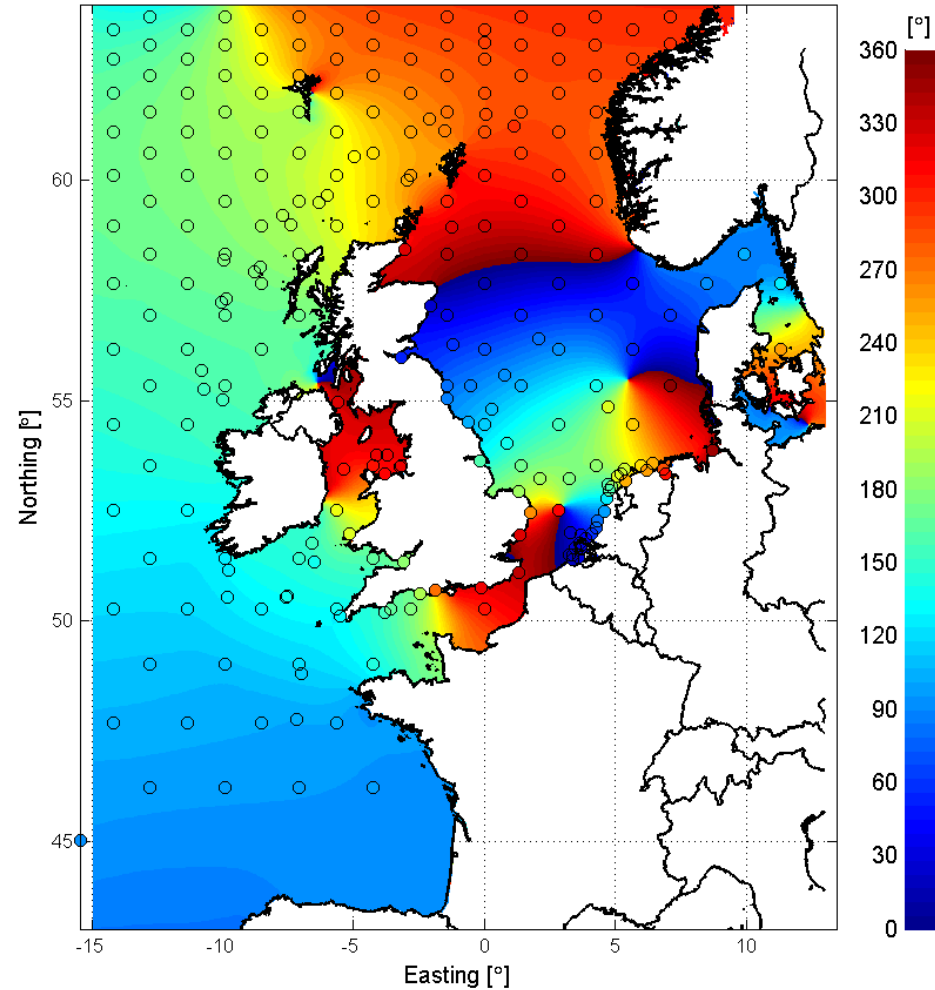
Student project.  
Delft3d at <http://oss.deltares.nl>

# Tides in North Sea

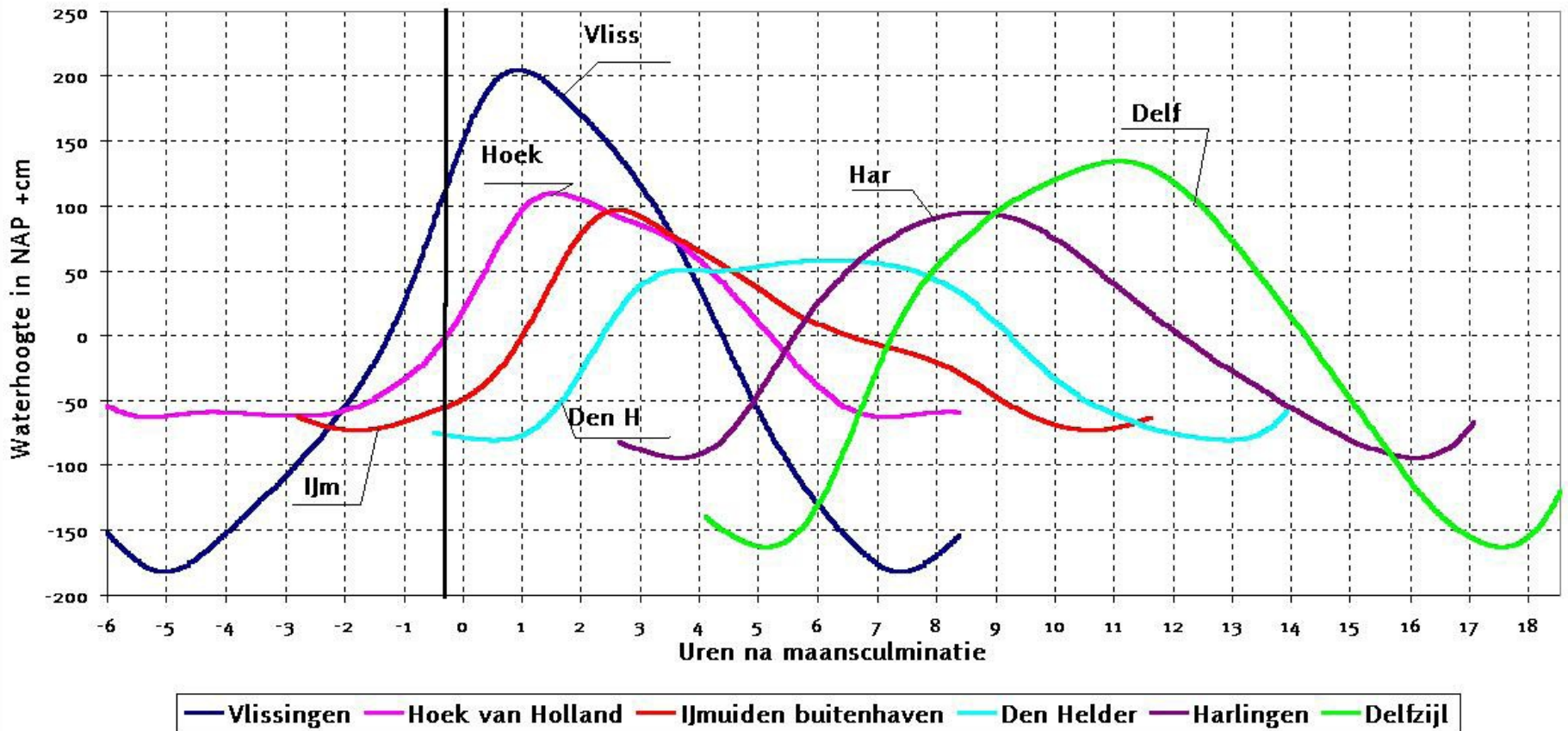
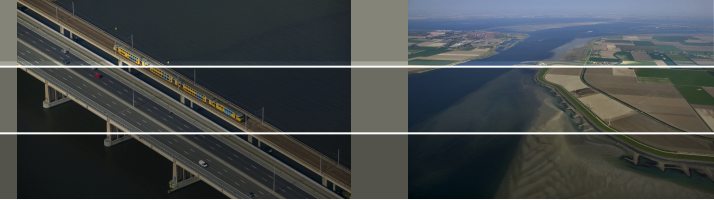
Amplitude for constituent: M2 (RMSE = 6.5 cm)



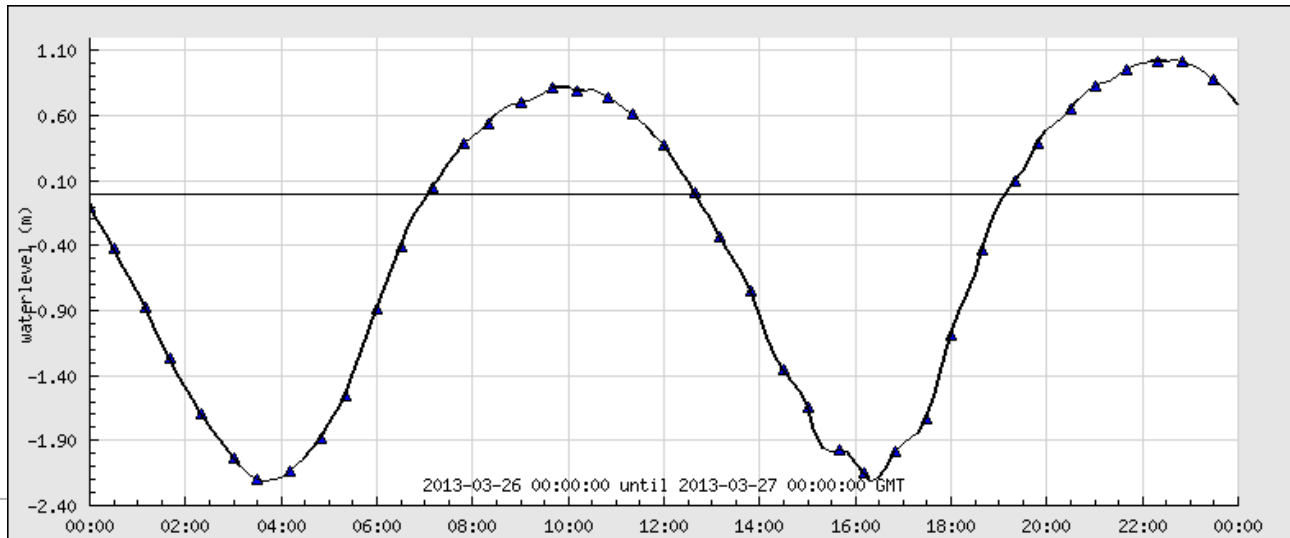
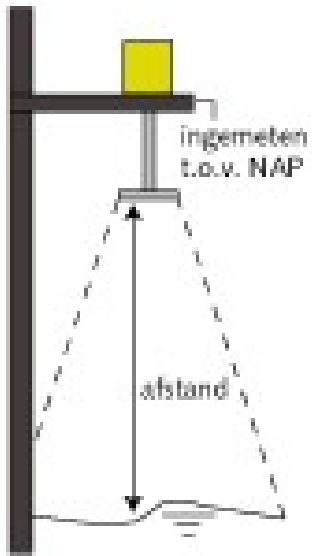
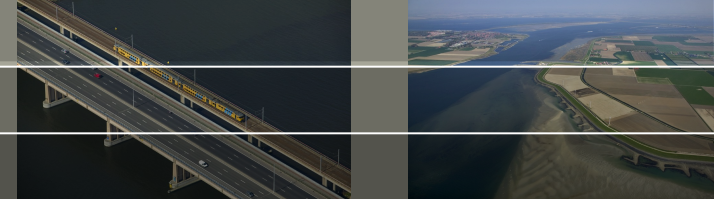
Phase for constituent: M2 (RMSE = 4.8 °)



# Tides along Dutch coast



# Radarnivometer

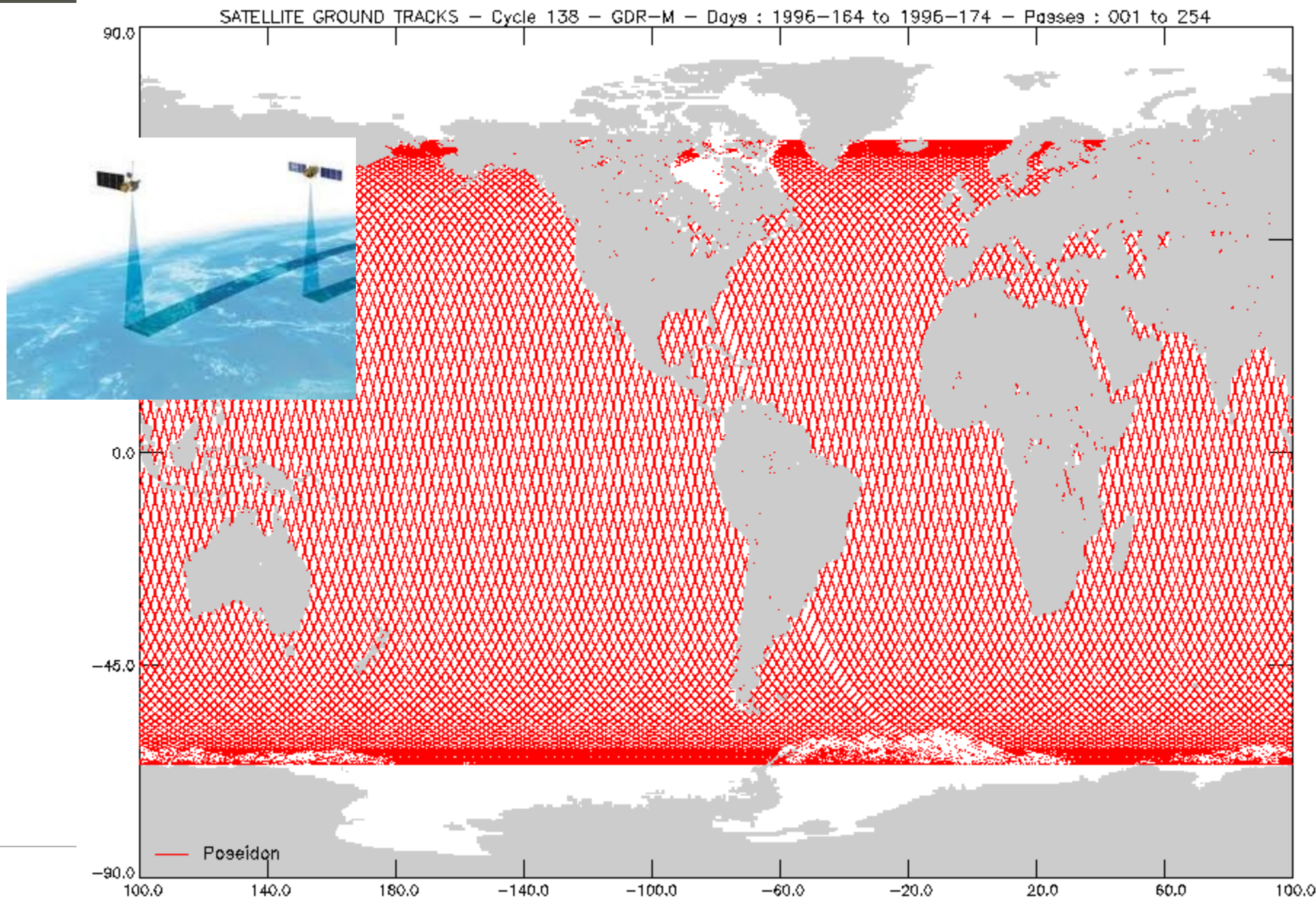
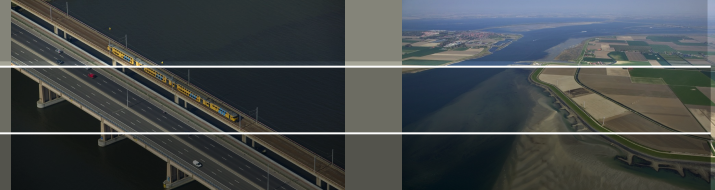


[http://www.rijkswaterstaat.nl/geotool/waterhoogte\\_tov\\_nap.aspx](http://www.rijkswaterstaat.nl/geotool/waterhoogte_tov_nap.aspx)

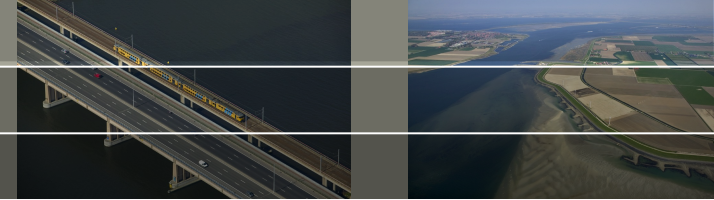
27 Mar 2013

**Deltares**

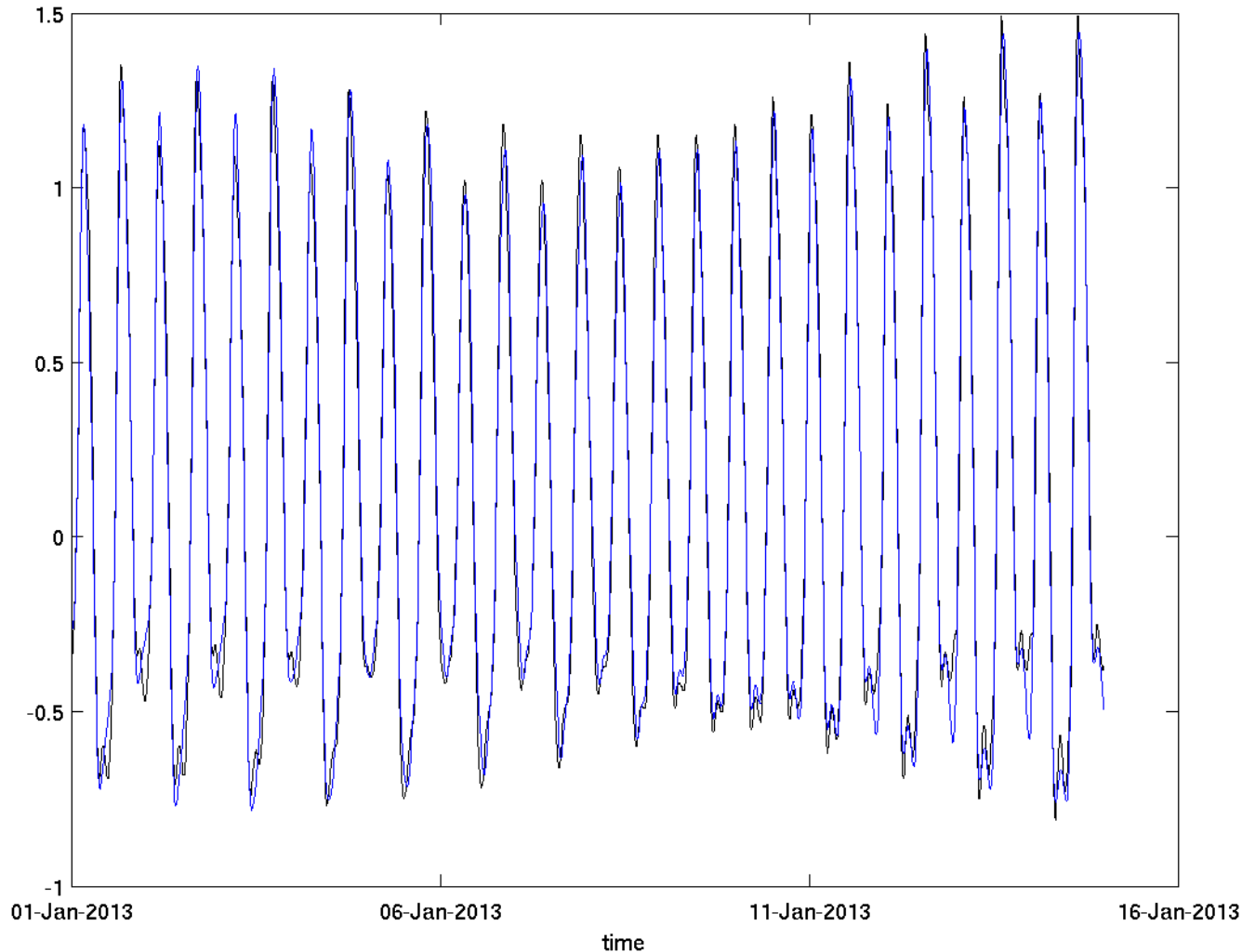
# Altimeter observations



# Harmonic analysis



Tides Hoek van Holland ,M2,S2,M4,N2,O1,MS4,A0,SA,MU2,K1,2MN2,MN4,K2,NU2,M6,Q1,2MS6,MK4,P1,3MS8



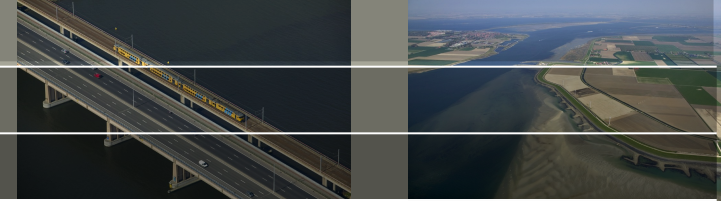
20 constituents  
out of 95 in  
analysis

Needs at least 1 year of data

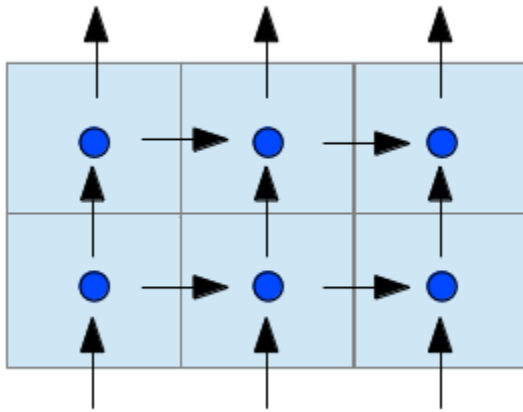
NCG 6 Feb 2014



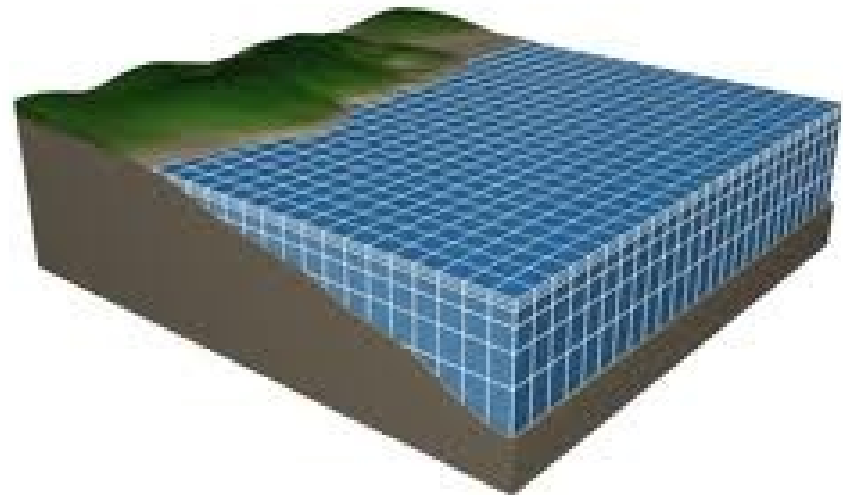
# Numerical models



2D-Grid

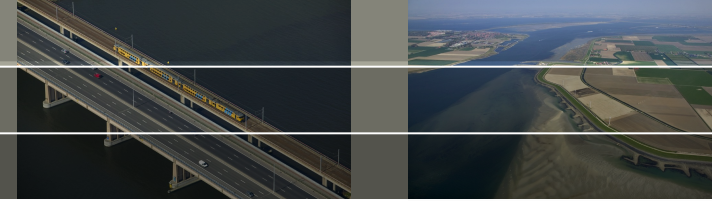


3-D Grid on the Coastal Ocean

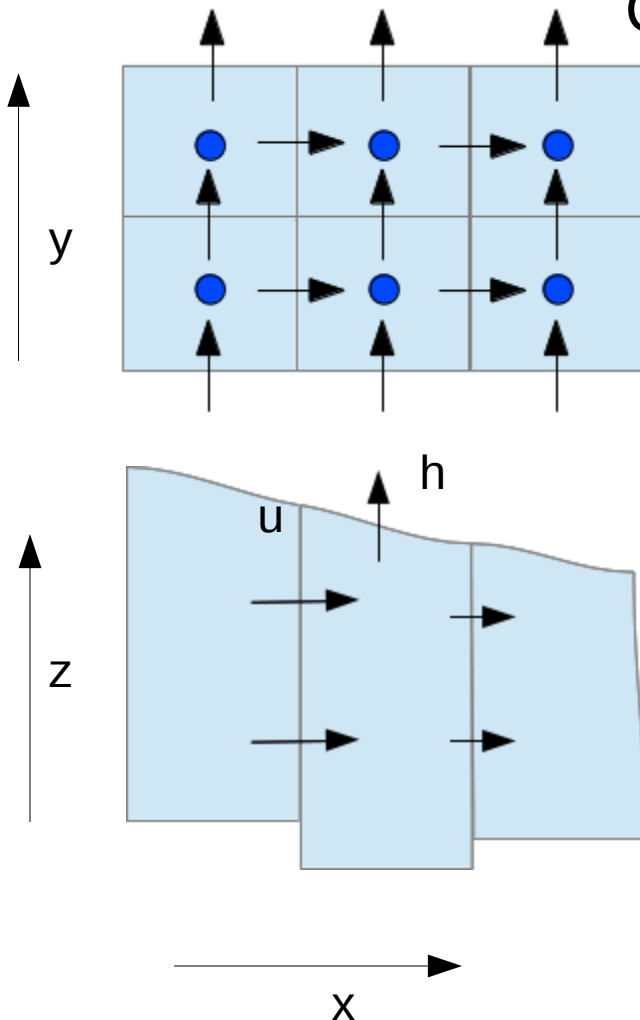


©The COMET Program

# Shallow water model



## Conservation of mass



Inflow

Level rise

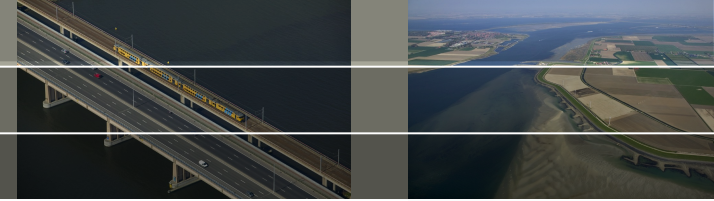
$$\Delta t H (u(x) - u(x + \Delta x)) \Delta y = \Delta h \Delta x \Delta y$$

$$\frac{\Delta h}{\Delta t} + \frac{H(u(x + \Delta x) - u(x))}{\Delta x} = 0$$

$$\frac{\partial h}{\partial t} + \frac{\partial H u}{\partial x} + \frac{\partial H v}{\partial y} = 0$$

Note: non-linearity

# Shallow water model



Conservation of momentum in x-direction

$$\frac{\partial u}{\partial t} + g \frac{\partial h}{\partial x} - f v + \frac{cu}{H} + \frac{\partial \Phi'}{\partial x} = 0$$

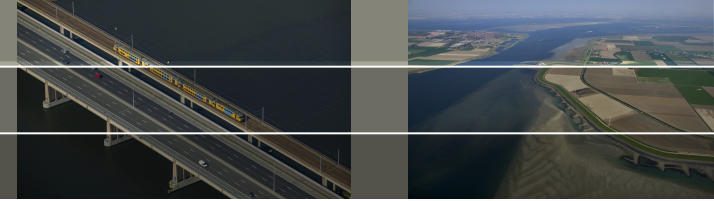
$$M a = F$$

$$\frac{\partial u}{\partial t} = -g \frac{\partial h}{\partial x} + f v - \frac{cu}{H} - \frac{\partial \Phi'}{\partial x}$$

↓  
acceleration

- Tidal potential
- Friction
- Coriolis 'force'
- Surface slope

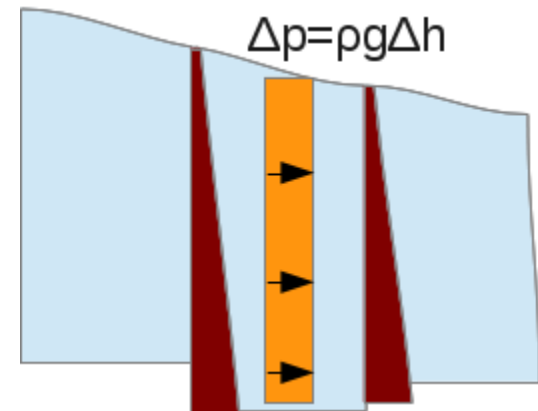
# Hydrostatic pressure



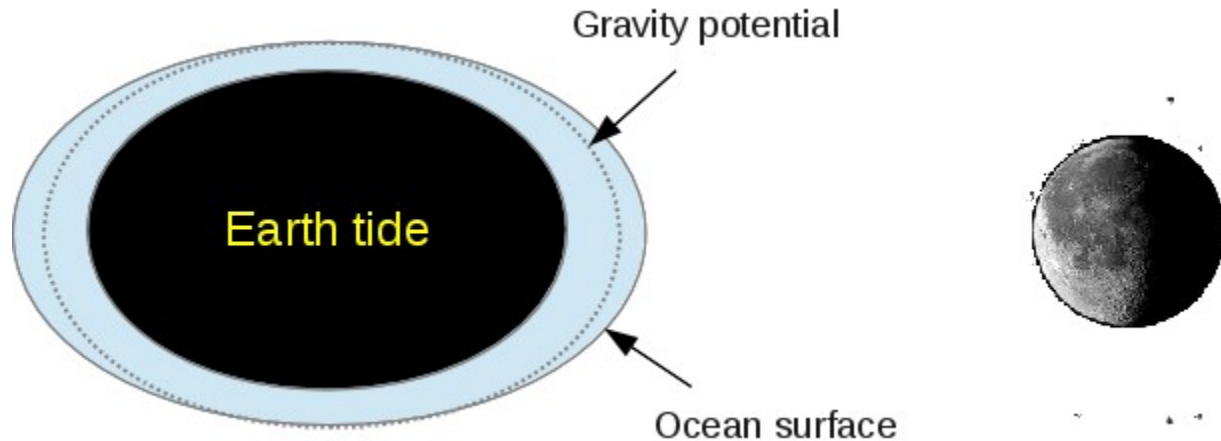
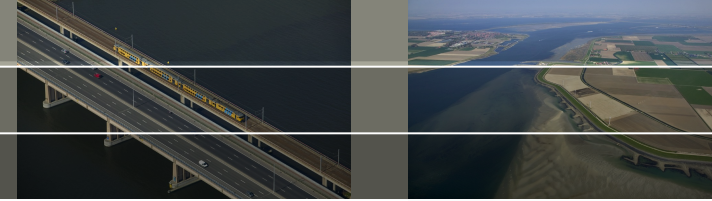
Surface slope

$$p = p_0 + \rho g(z - h)$$

$$F = \rho g H (h(x + \Delta x) - h(x))$$



# Tidal potential



$$\Phi = \frac{GM}{|x - x_m|}$$

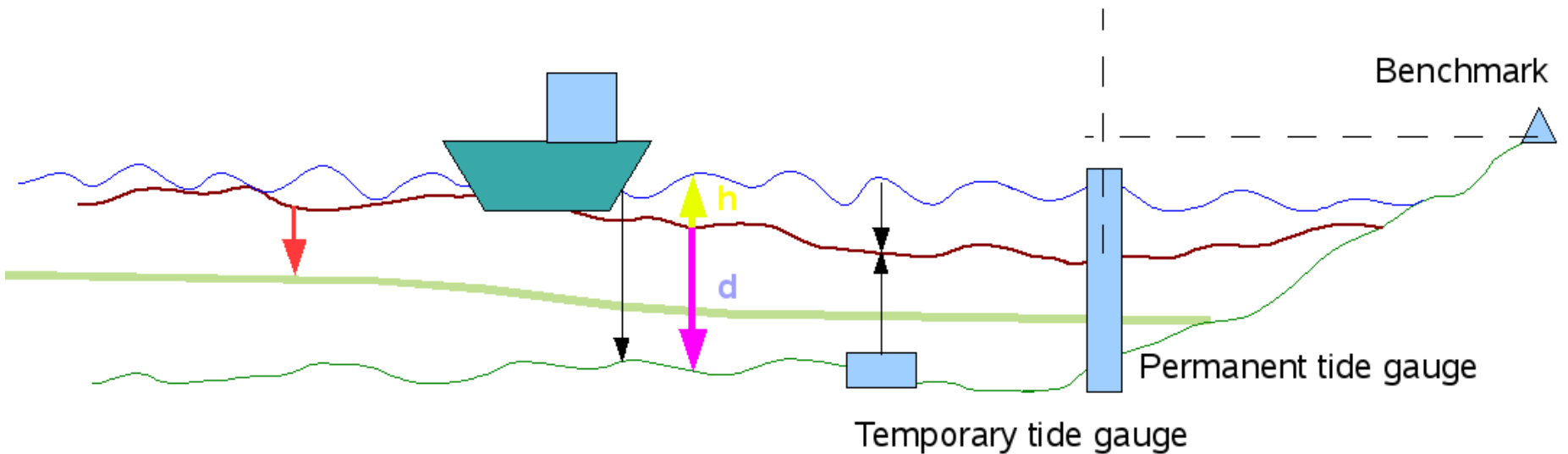
$$F = -\nabla \Phi m$$

$$\Phi_{eff} = \Phi' (1 + k - h)$$

h=0.6 earth tide

k=0.3 change in earth's potential

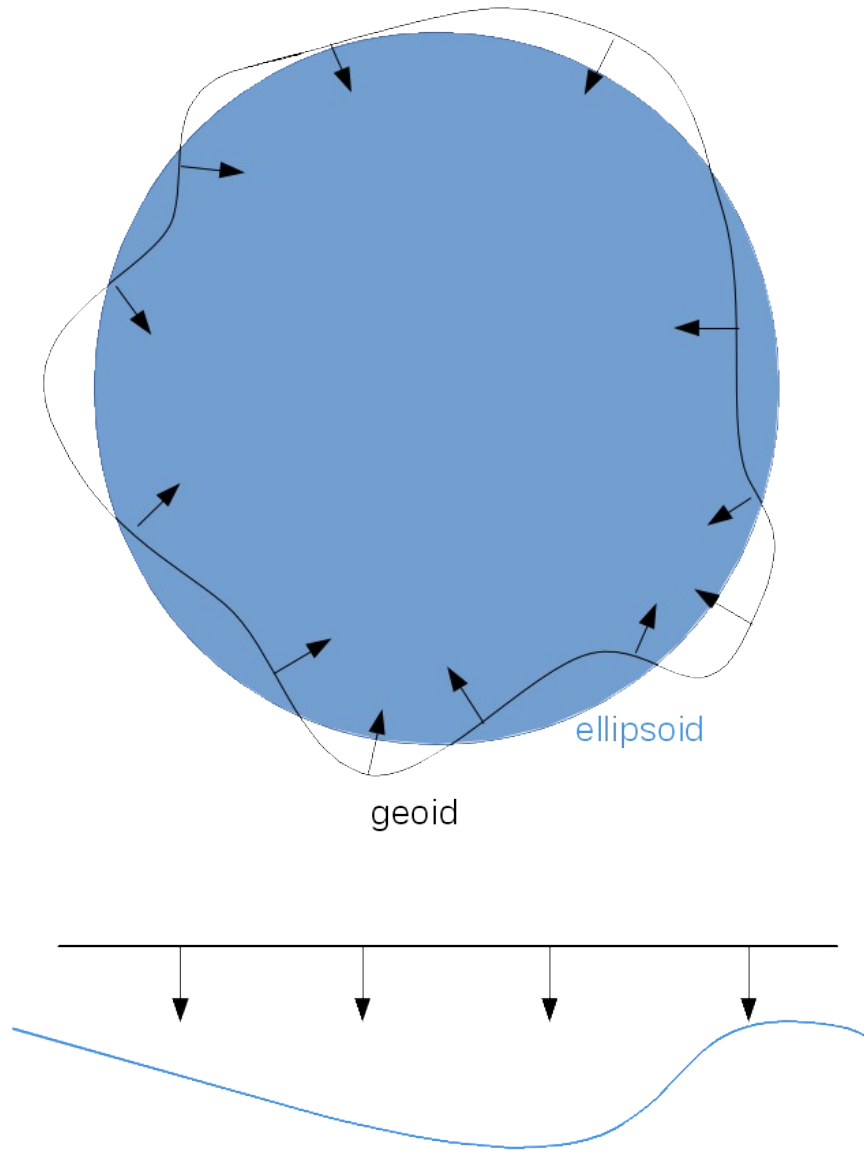
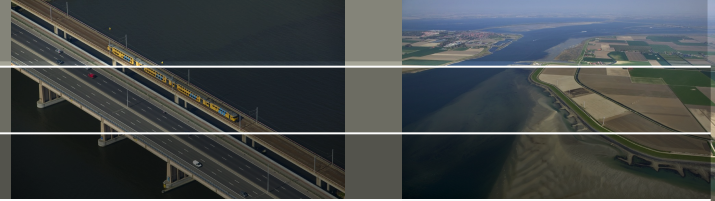
- MSL
- Sea Surface
- Bottom
- LAT



Source: [citg.tudelft.nl](http://citg.tudelft.nl)

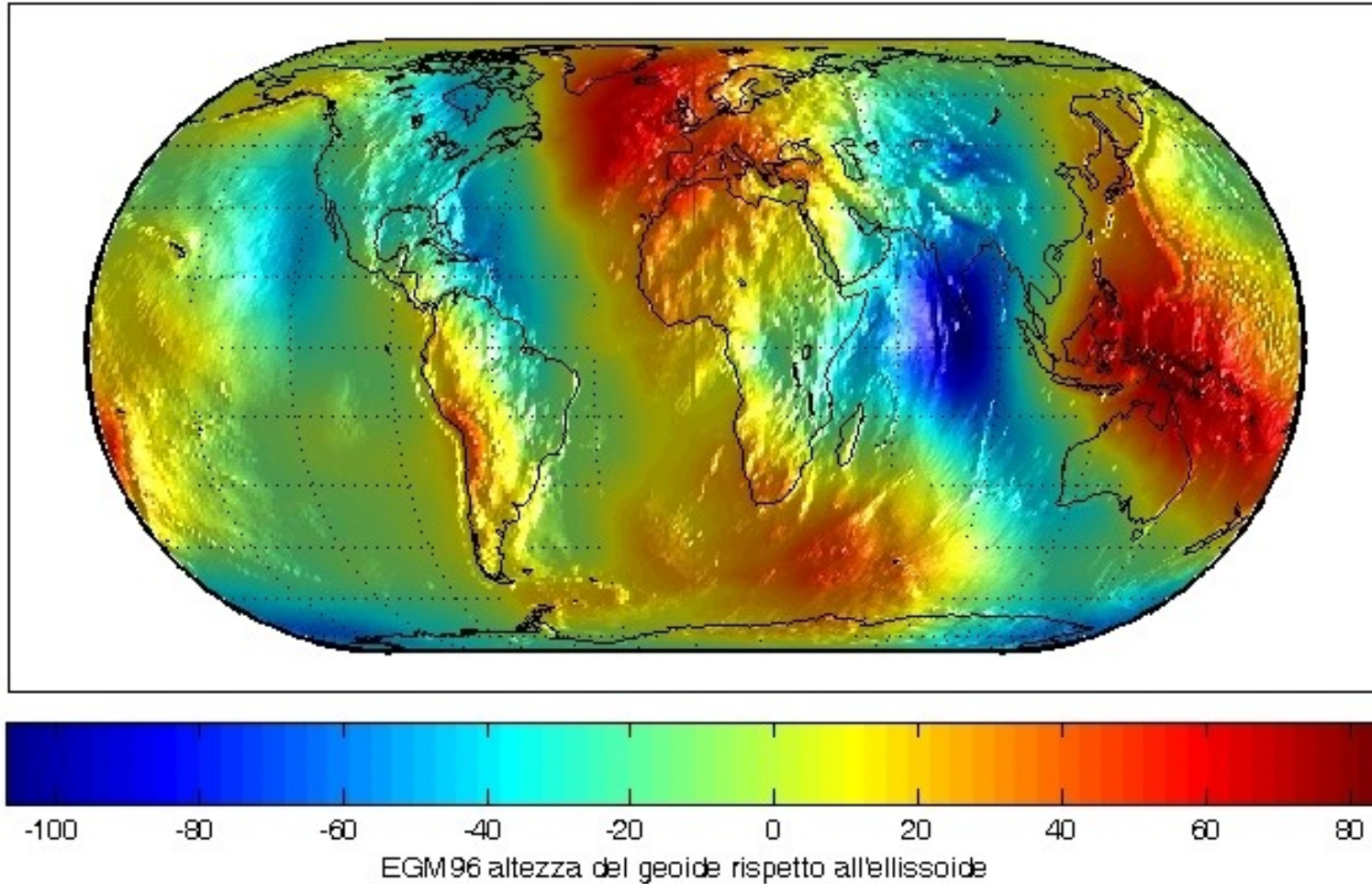
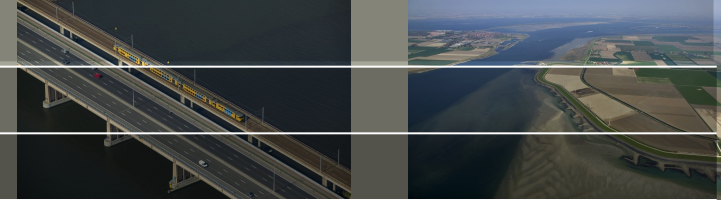


# Geoid in numerical model



Gravity perpendicular to geoid

# Geoid relative to ellipsoid

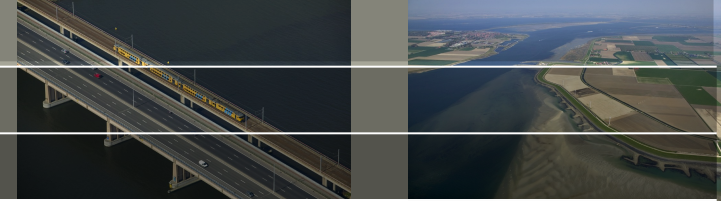


Source: cnes

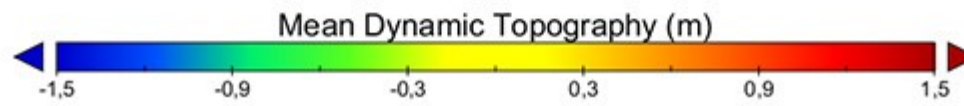
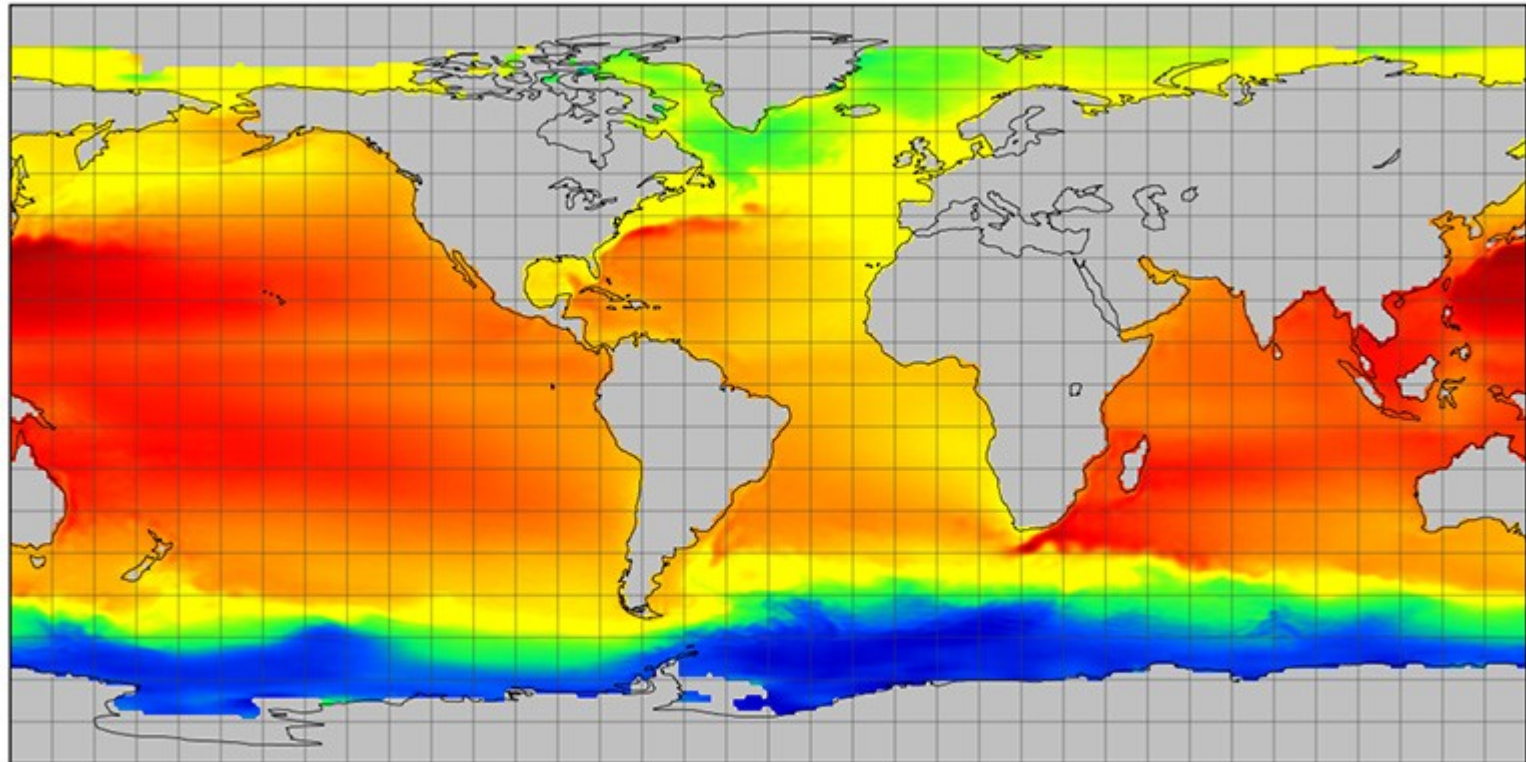
**Deltares**



# Mean dynamic topography

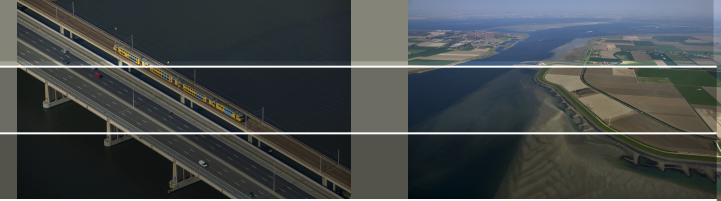


Mean Dynamic Topography

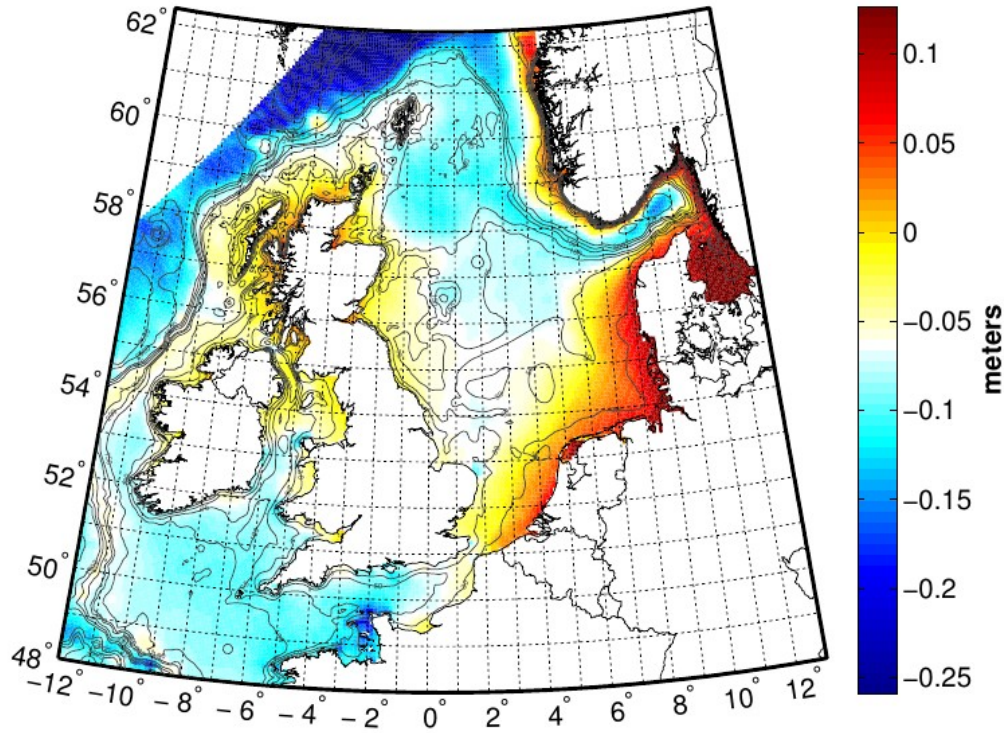


Data Min = -1.7, Max = 9999.0

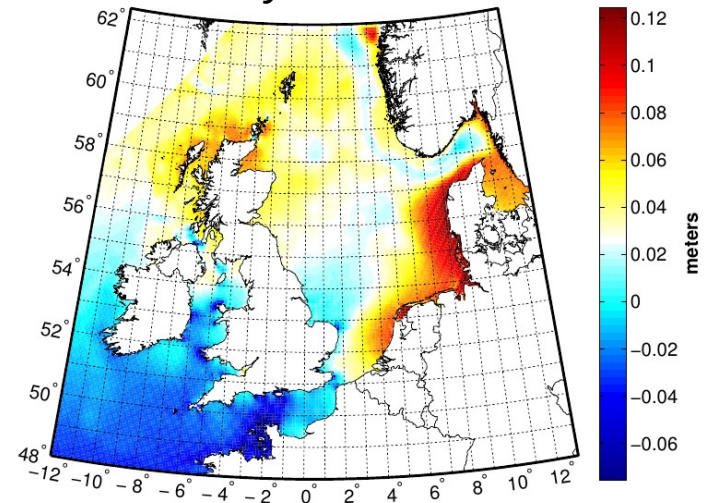
# Mean dynamic topography



MDT wrt EGG08

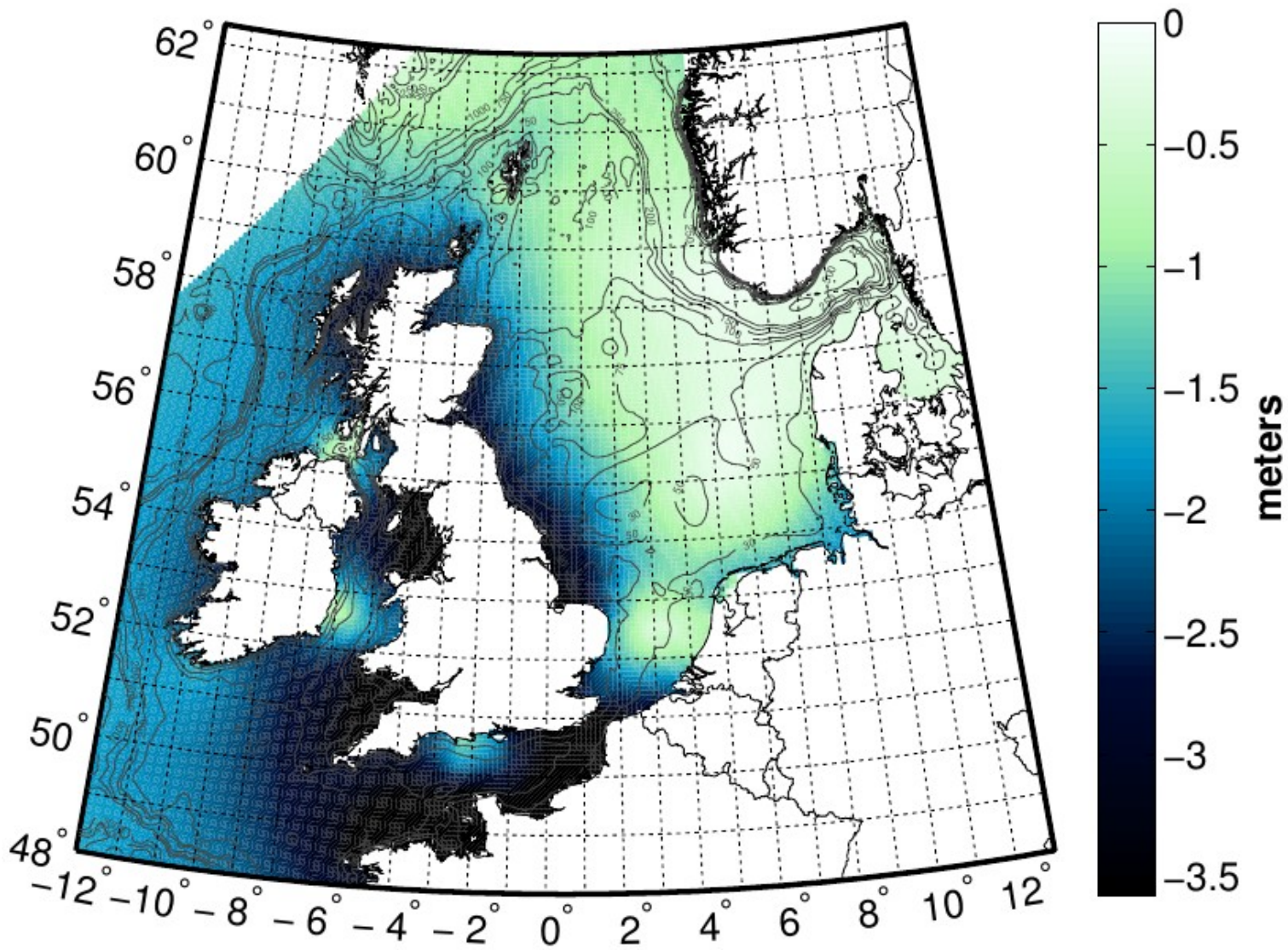


Density contribution

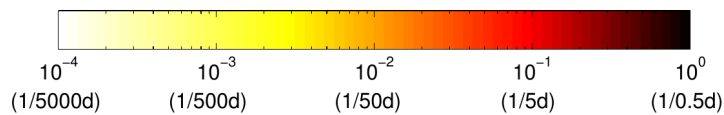
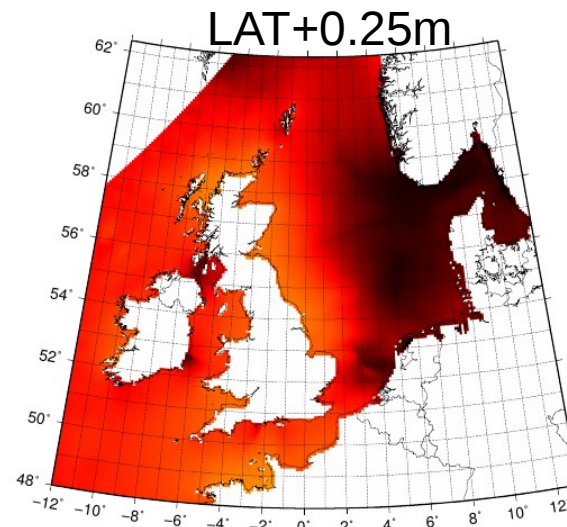
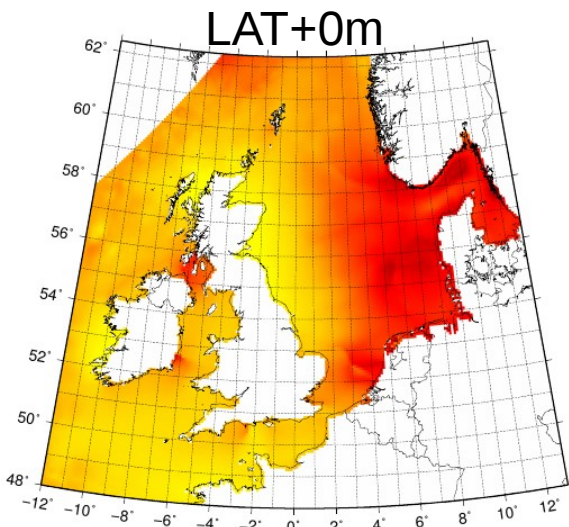
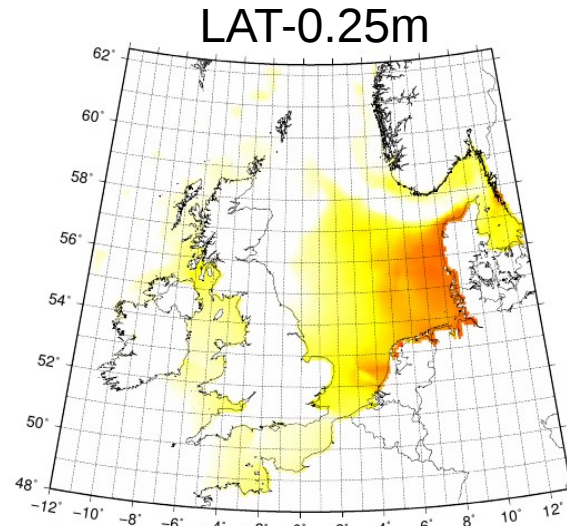
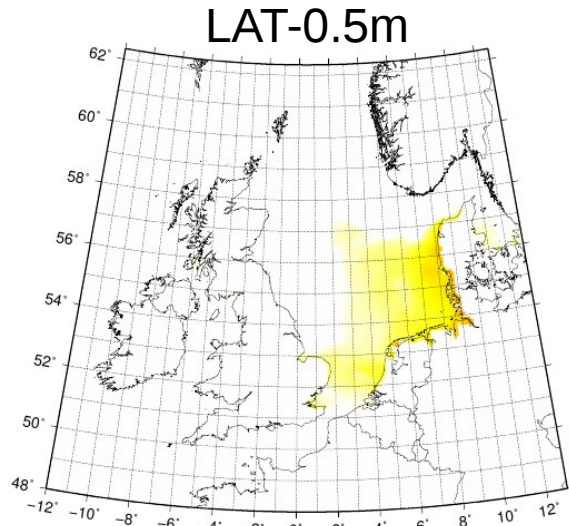
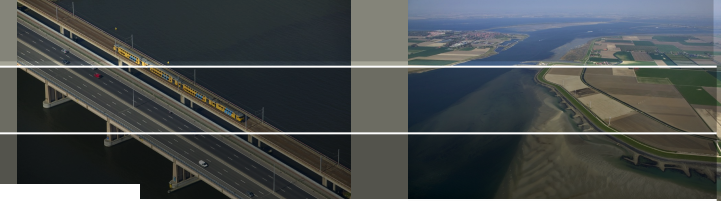


Source: Slobbe et. al. 2012

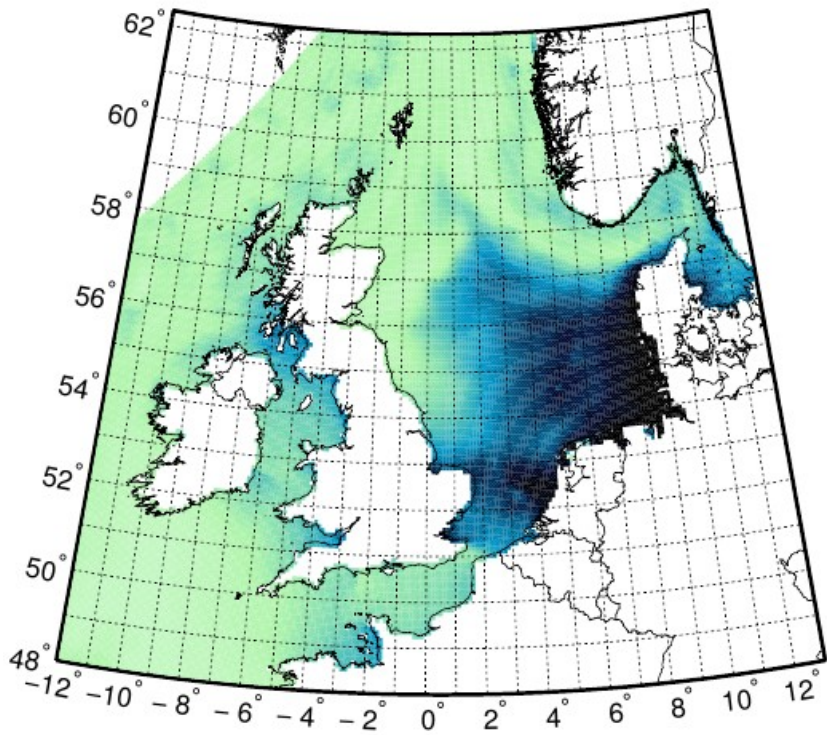
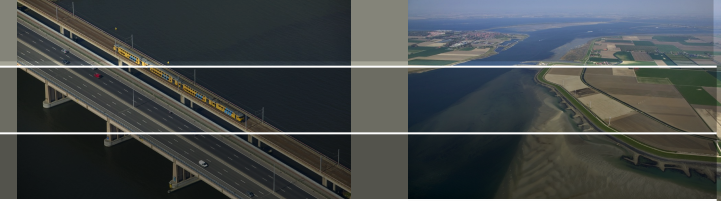
# Lowest Astronomical Tide



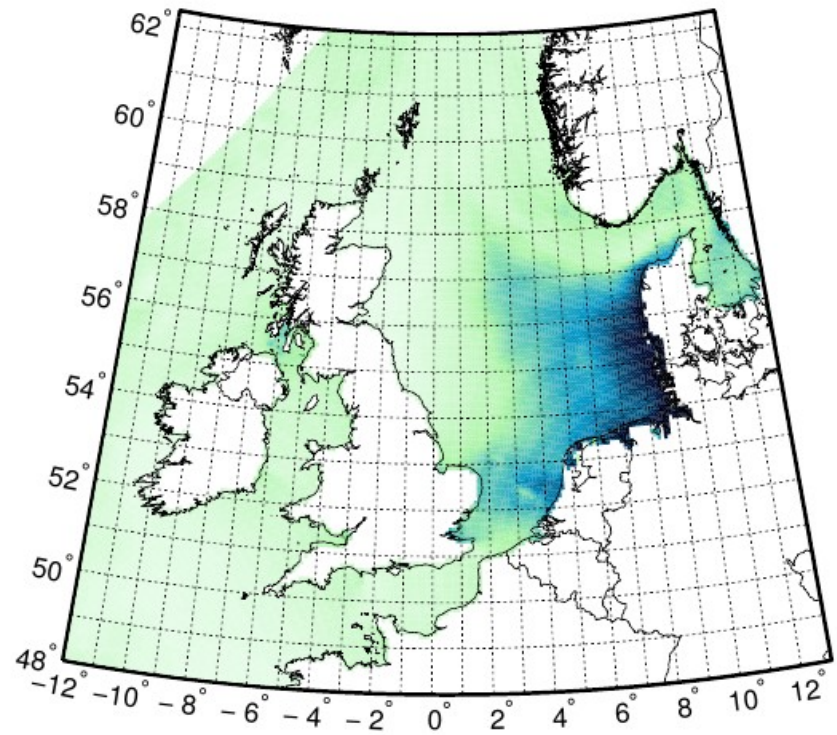
# LAT exceedance frequency



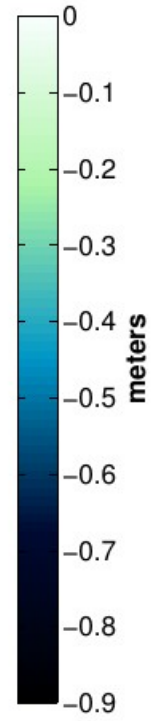
# LAT exceedance frequency



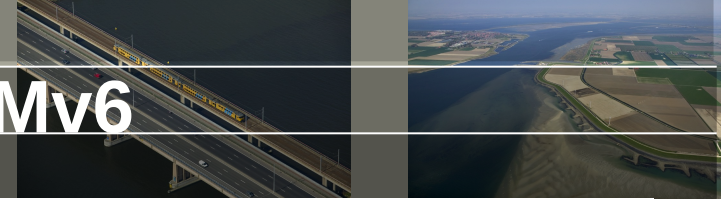
(b) Once per 10 years



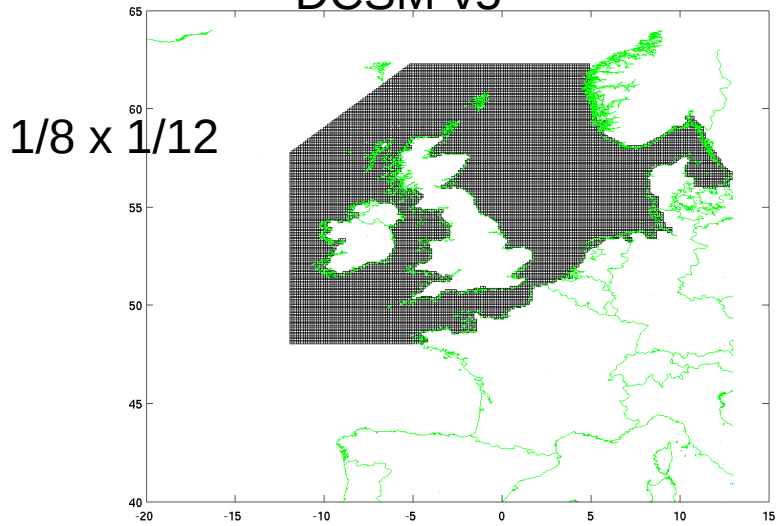
(c) Once per year



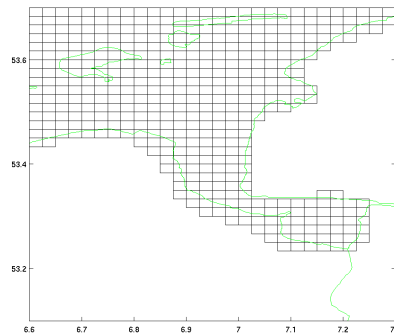
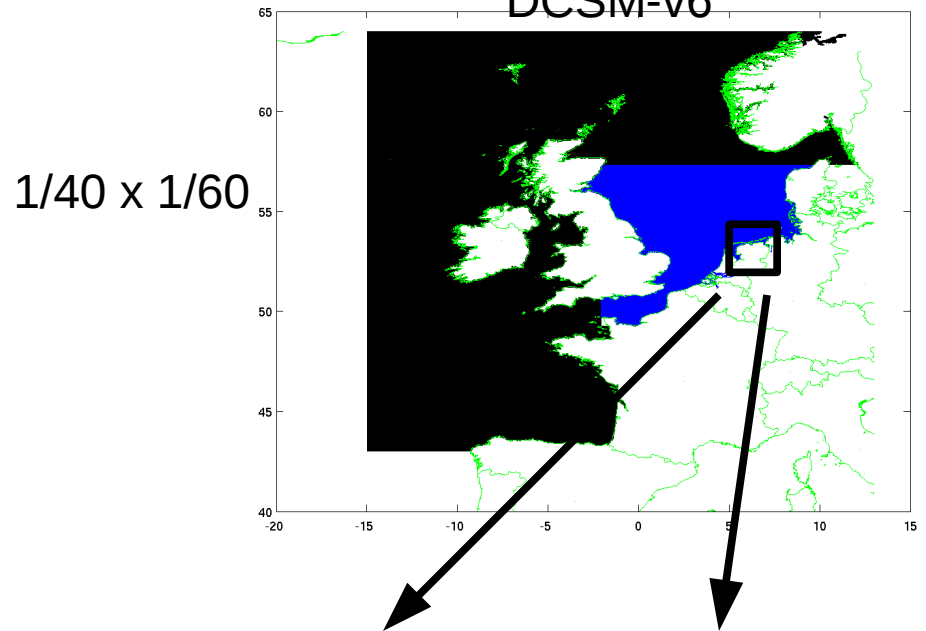
# New surge & tide model – DCSMv6



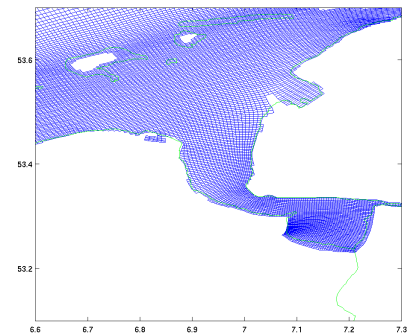
DCSM-v5



DCSM-v6



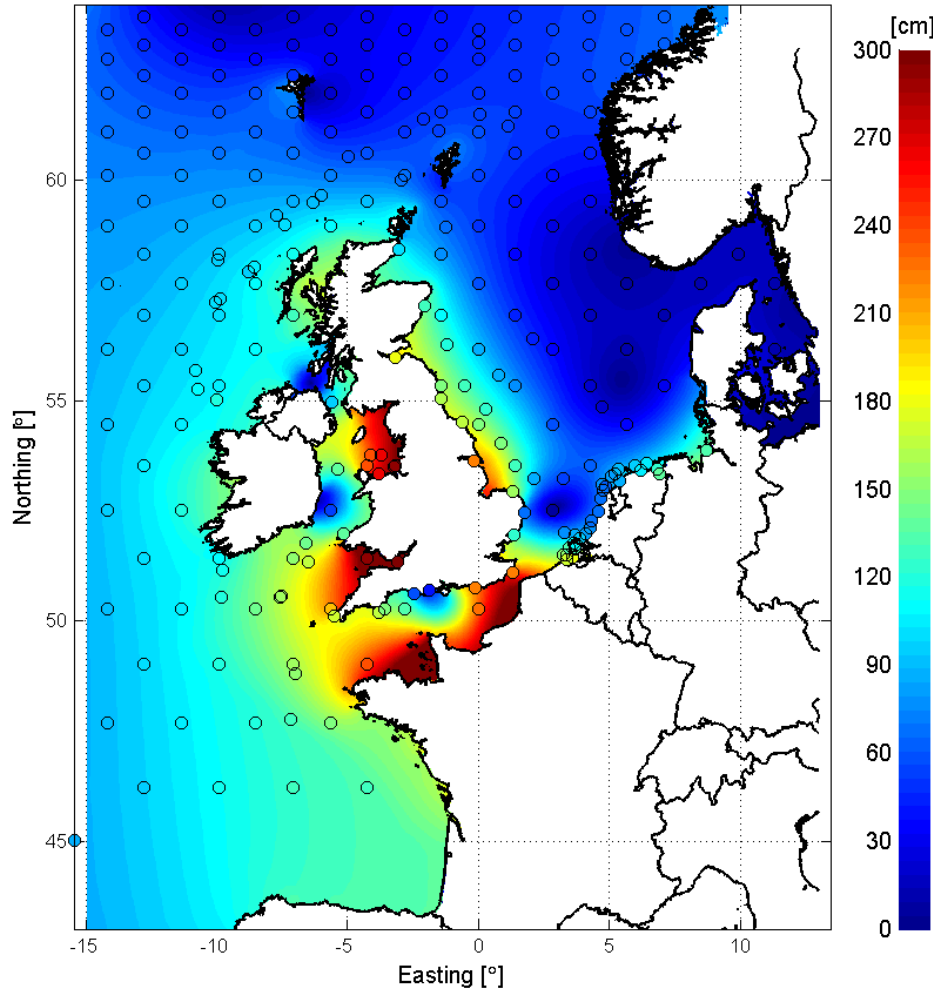
domain 1 detail



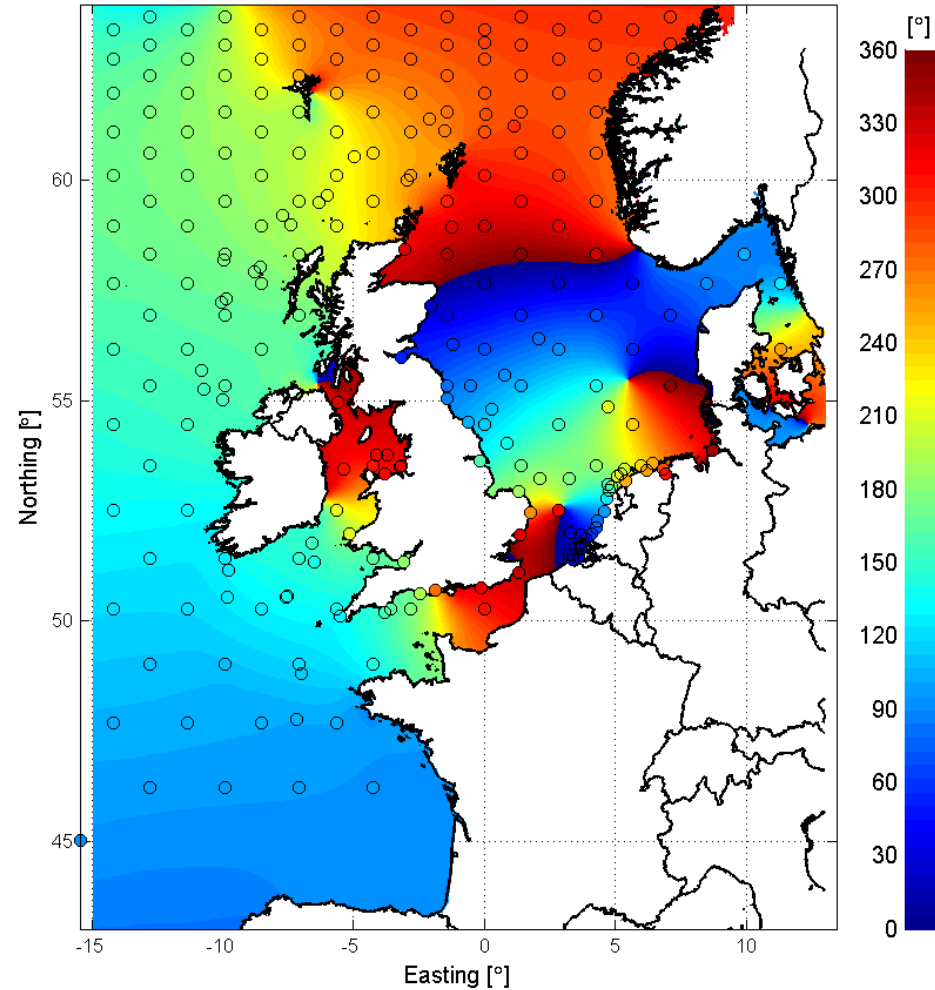
domain 2 detail

# Calibration of tides

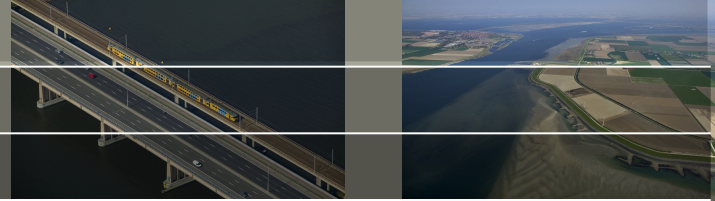
Amplitude for constituent: M2 (RMSE = 6.5 cm)



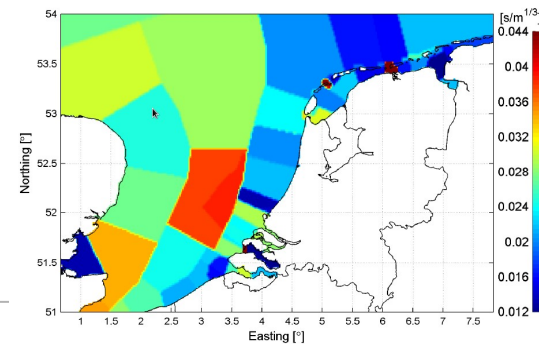
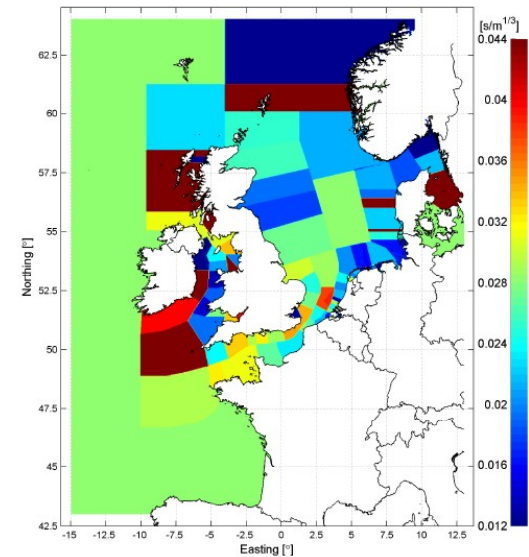
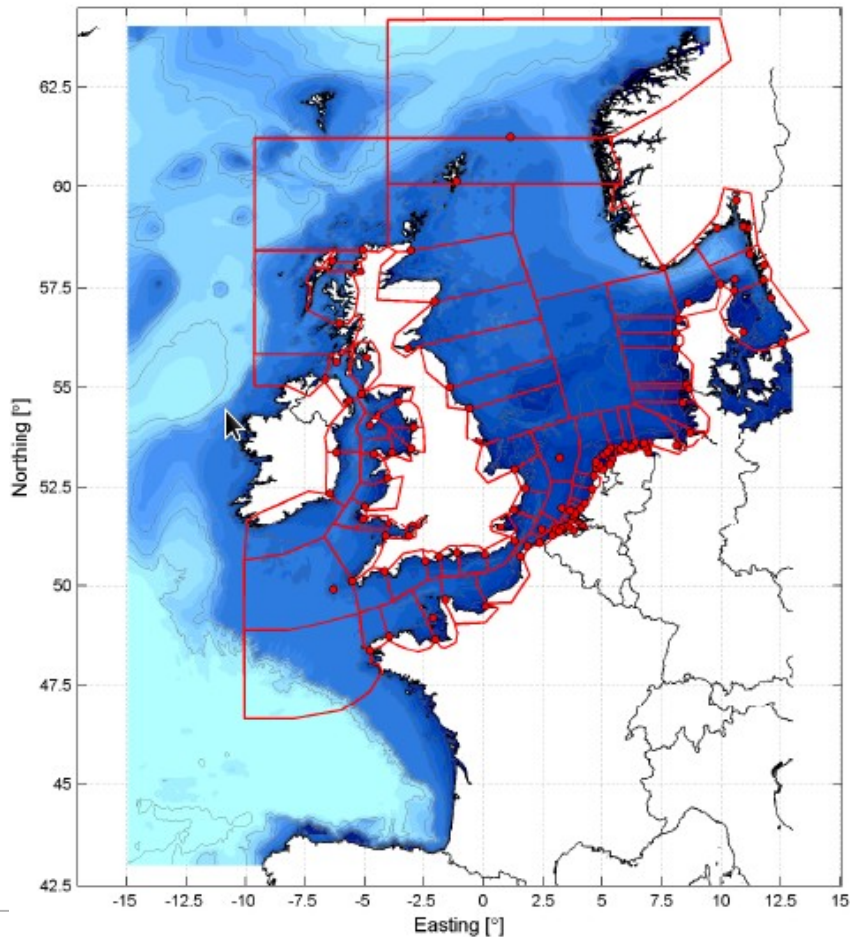
Phase for constituent: M2 (RMSE = 4.8 °)



# Calibration of tides



- More than 100 tide gages used
- Around 100 parameters for friction and 100 parameters for depth
- Efficient optimization methods with restarting and parallel computing

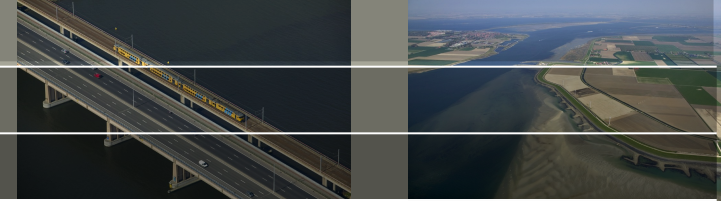


OpenDA  
www.openda.org

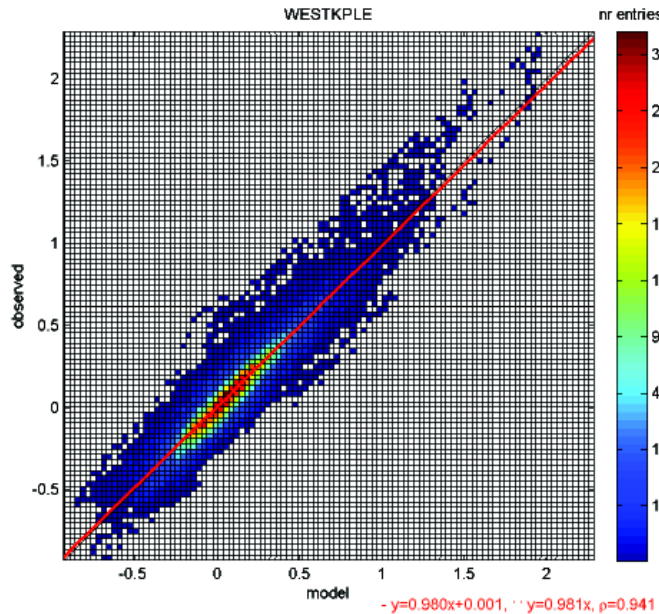
Deltares



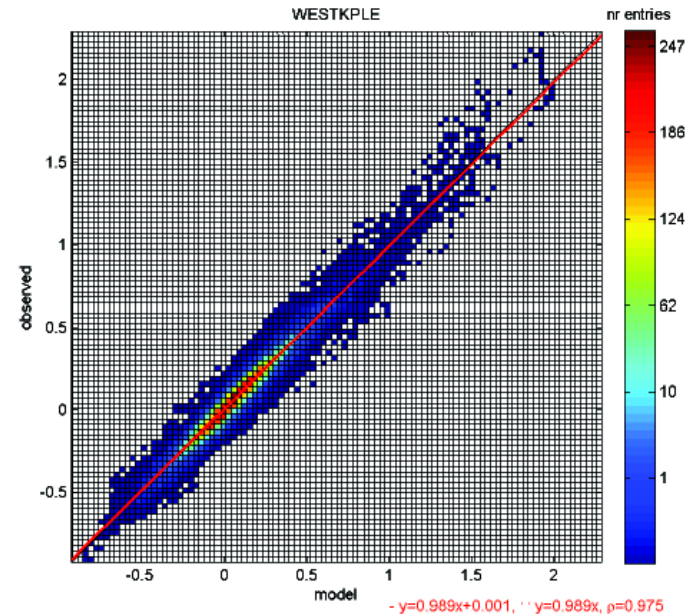
# Results calibration DCSM-v6



|                    | RMSE tides | RMSE surge | RMSE sea-level |
|--------------------|------------|------------|----------------|
| Before calibration | 6.6        | 9.7        | 11.7           |
| After calibration  | 3.7        | 6.9        | 7.8            |

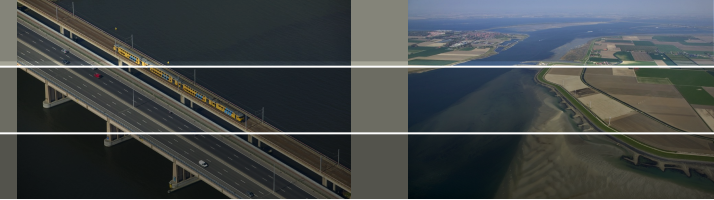


Surge before calibration



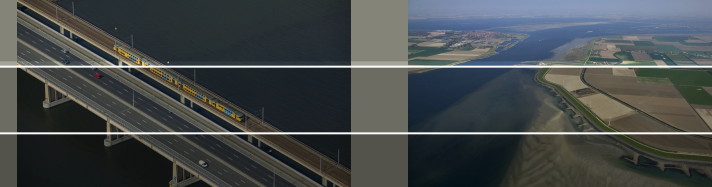
Surge after calibration

# DCSM v5 and v6



| Station      | RMSE tide (cm) |        |     | RMSE surge (cm) |        |     | RMSE water level (cm) |        |     |
|--------------|----------------|--------|-----|-----------------|--------|-----|-----------------------|--------|-----|
|              | DCSMv5         | DCSMv6 | (%) | DCSMv5          | DCSMv6 | (%) | DCSMv5                | DCSMv6 | (%) |
| CADZD        | 12.6           | 3.7    | -71 | 10.8            | 7.0    | -35 | 16.6                  | 7.9    | -52 |
| WESTKPLE     | 10.4           | 3.2    | -69 | 10.4            | 6.6    | -37 | 14.7                  | 7.3    | -50 |
| ROOMPBTN     | 14.2           | 3.0    | -79 | 9.5             | 6.6    | -31 | 17.1                  | 7.2    | -58 |
| BROUWHVSGT08 | 8.3            | 3.3    | -60 | 9.4             | 6.8    | -28 | 12.6                  | 7.6    | -40 |
| HARVT10      | 8.2            | 3.2    | -61 | 9.5             | 7.0    | -26 | 12.6                  | 7.7    | -39 |
| HOEKVHLD     | 8.0            | 3.8    | -53 | 9.1             | 6.8    | -25 | 12.2                  | 7.8    | -36 |
| SCHEVNGN     | 10.2           | 3.3    | -68 | 8.6             | 7.0    | -19 | 13.3                  | 7.7    | -42 |
| IJMDBTHVN    | 7.5            | 3.7    | -51 | 8.9             | 7.3    | -18 | 11.7                  | 8.1    | -31 |
| PETTZD       | 9.9            | 4.2    | -58 | 8.8             | 7.2    | -18 | 13.2                  | 8.3    | -37 |
| K13APFM      | 8.2            | 3.0    | -63 | 7.1             | 5.4    | -24 | 10.8                  | 6.2    | -43 |
| TERSLNZE     | 6.8            | 3.9    | -43 | 8.2             | 7.2    | -12 | 10.7                  | 8.2    | -23 |
| WIERMGDN     | 7.7            | 4.4    | -43 | 8.3             | 7.1    | -14 | 11.4                  | 8.4    | -26 |
| HUIBGT       | 8.6            | 4.2    | -51 | 8.5             | 7.4    | -13 | 12.1                  | 8.5    | -30 |
| average      | 9.3            | 3.6    | -61 | 9.0             | 6.9    | -23 | 13.0                  | 7.8    | -40 |
| RMS          | 9.5            | 3.7    | -61 | 9.1             | 6.9    | -24 | 13.1                  | 7.8    | -40 |

# Effects of ZUNO domain & tidal correction

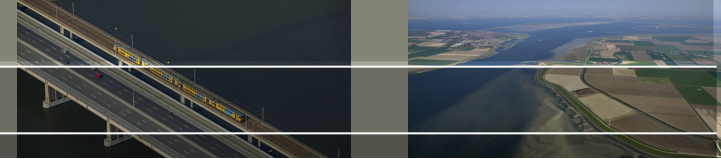


| DSCMv6     | RMSE tide | 2007   |      |
|------------|-----------|--------|------|
|            |           | RMSE   |      |
|            |           | zonder | met  |
| datum      |           |        |      |
| WICK       | 6.4       | 8.6    | 8.0  |
| ABDN       | 4.9       | 7.6    | 8.9  |
| NORTHSS    | 6.1       | 9.2    | 9.9  |
| LOWST      | 3.8       | 7.8    | 8.3  |
| SHEERNS    | 16.9      | 20.9   | 13.4 |
| DOVR       | 7.9       | 10.1   | 10.5 |
| CADZD      | 3.7       | 7.9    | 8.8  |
| VLISSGN    | 4.1       | 8.7    | 9.2  |
| HOEKVHLD   | 3.8       | 7.8    | 8.6  |
| IJMDBTHVN  | 3.7       | 8.1    | 9.7  |
| EURPFM     | 4.1       | 7.4    | 7.5  |
| HUIBGT     | 4.2       | 8.5    | 10.3 |
| HARLGN     | 7.0       | 11.3   | 12.3 |
| DELFLZL    | 11.9      | 17.8   | 14.6 |
| gemiddelde | 6.3       | 10.1   | 10.0 |
| RMS        | 7.3       | 10.9   | 10.2 |

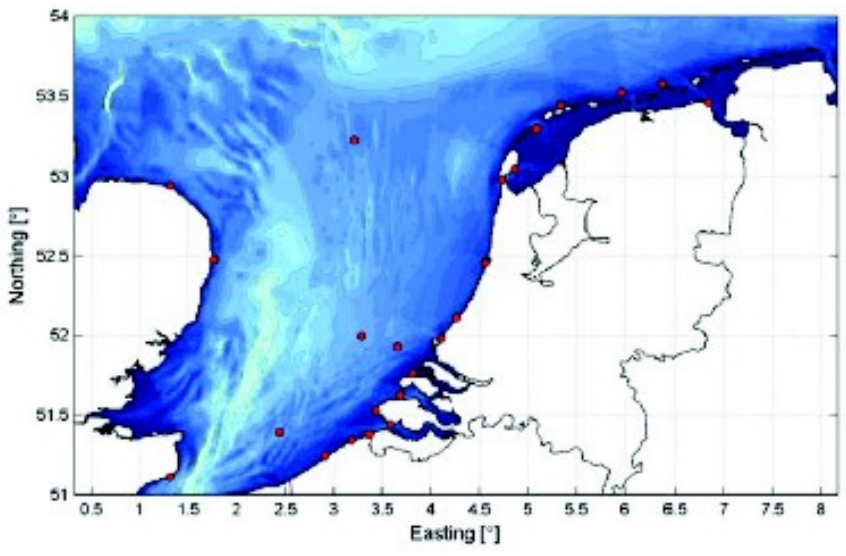
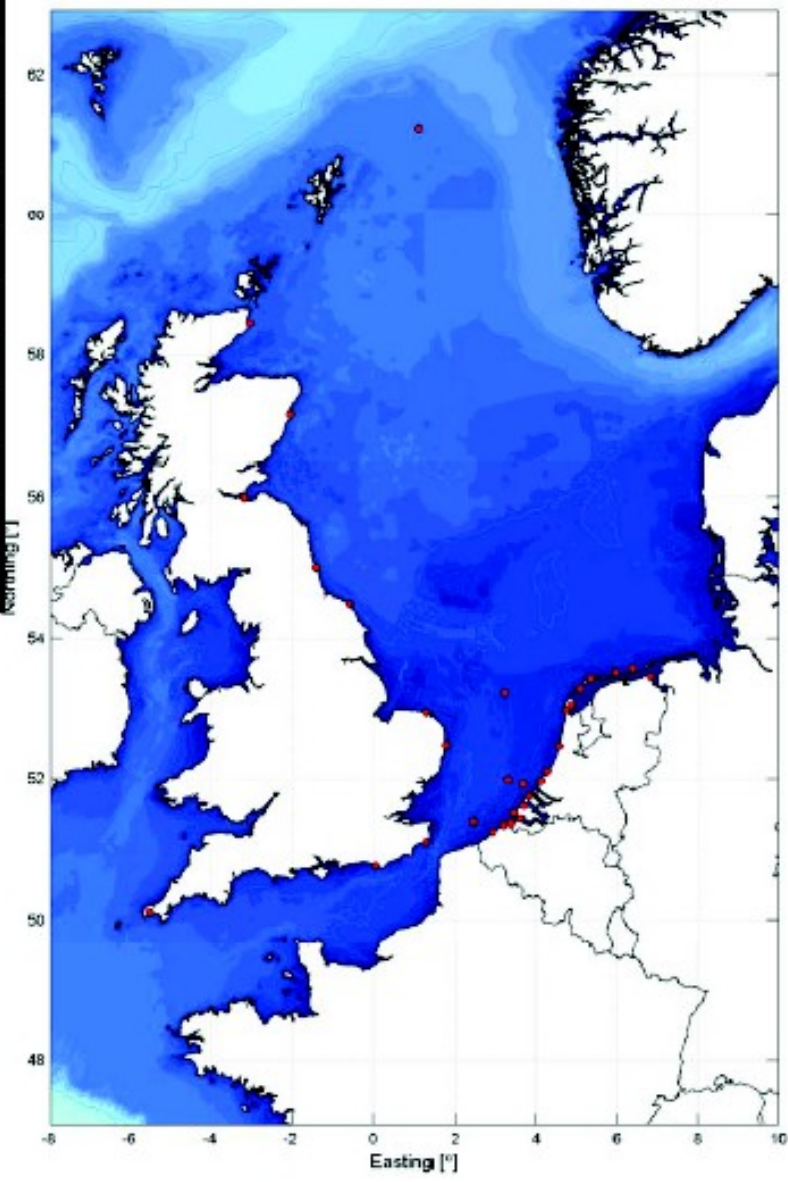


| DCSMv6 +ZUNO | RMSE tide | 2007   |      |
|--------------|-----------|--------|------|
|              |           | RMSE   |      |
|              |           | zonder | met  |
| datum        |           |        |      |
| WICK         | 5.8       | 8.6    | 9.3  |
| ABDN         | 5.3       | 8.7    | 10.8 |
| NORTHSS      | 5.3       | 9.6    | 12.1 |
| LOWST        | 3.7       | 8.4    | 9.9  |
| SHEERNS      | 7.4       | 12.8   | 14.0 |
| DOVR         | 4.8       | 8.1    | 11.0 |
| CADZD        | 3.2       | 8.2    | 10.1 |
| VLISSGN      | 3.2       | 8.5    | 10.4 |
| HOEKVHLD     | 3.4       | 7.7    | 9.5  |
| IJMDBTHVN    | 3.3       | 8.1    | 10.3 |
| EURPFM       | 2.9       | 7.1    | 8.5  |
| HUIBGT       | 4.4       | 8.8    | 10.7 |
| HARLGN       | 3.9       | 8.1    | 11.2 |
| DELFLZL      | 4.6       | 10.4   | 13.4 |
| gemiddelde   | 4.4       | 8.8    | 10.8 |
| RMS          | 4.5       | 8.9    | 10.9 |

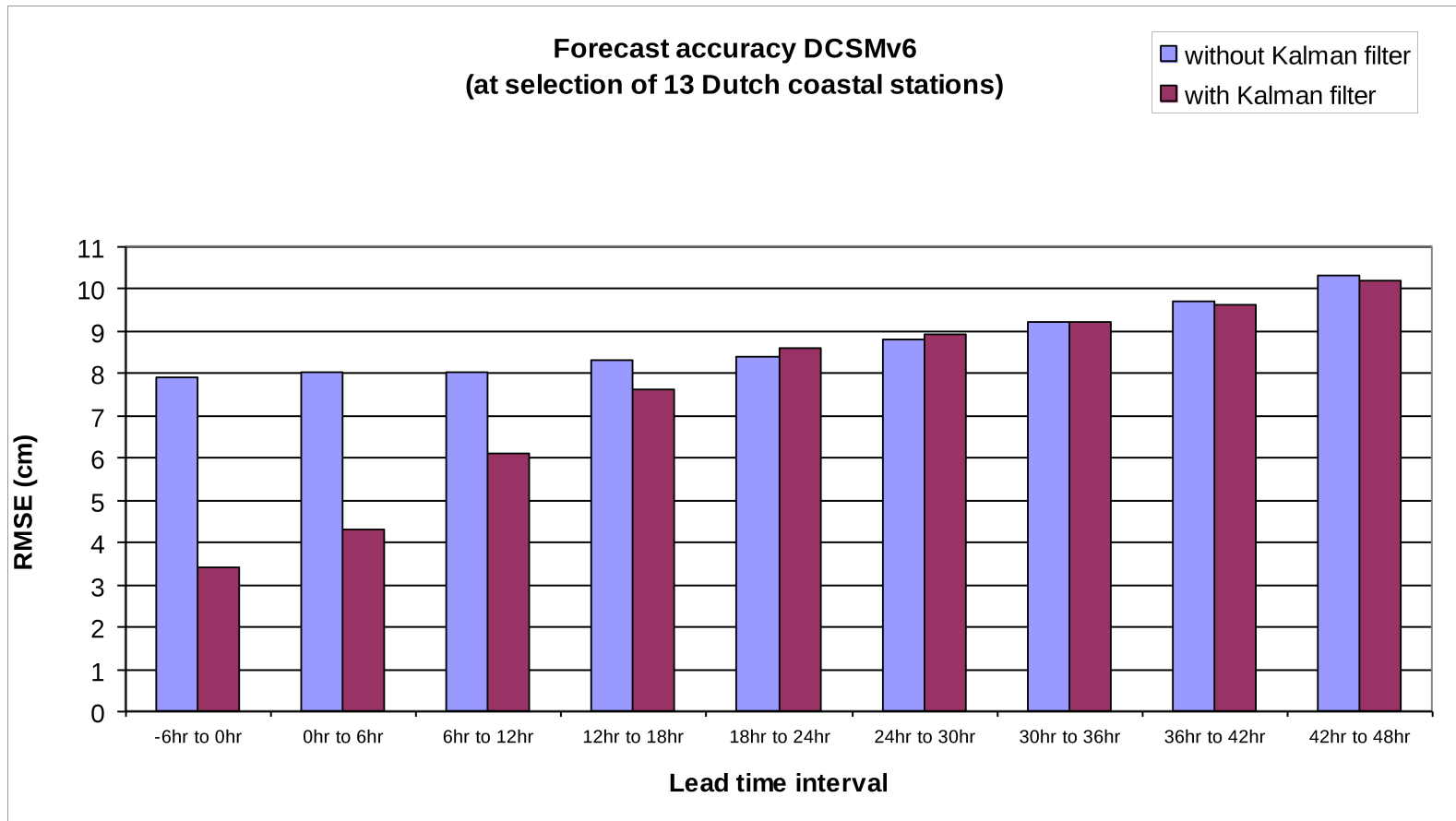
# Kalman filter for DCSMv6



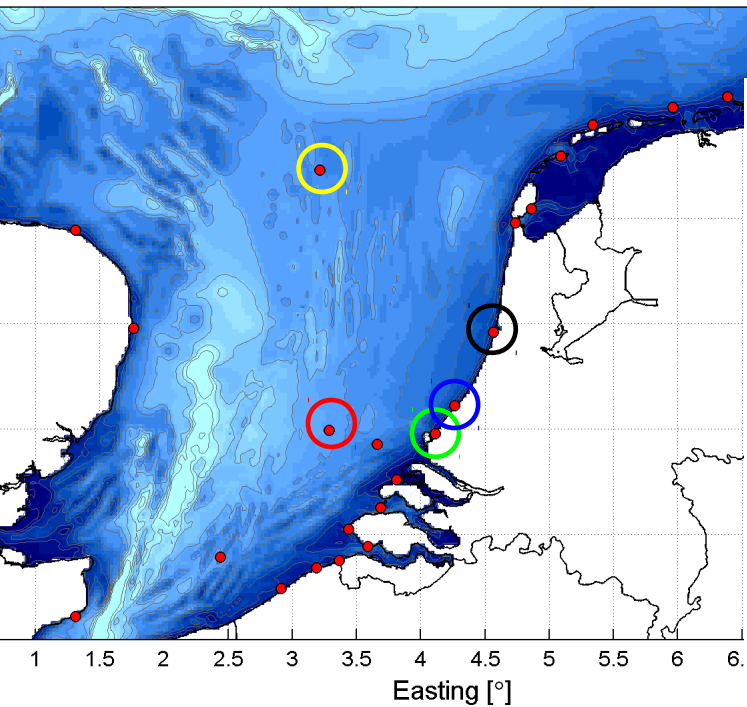
|            |              |          |
|------------|--------------|----------|
| NORTHCMRT  | CADZD        | HUIBGT   |
| WICK       | WESTKPLE     | NEWLN    |
| ABDN       | EURPFM       | NEWHVN   |
| LEITH      | BROUWHVSGT08 | DOVR     |
| NORTHSS    | LICHTELGRE   | VLISSGN  |
| WHITBY     | HOEKVHLD     | ROOMPBTN |
| CROMR      | SCHEVNGN     | DENHDR   |
| LOWST      | IJMDBTHVN    | OUUSD    |
| Oostende   | K13APFM      | VLIELHVN |
| Westhinder | TERSLNZE     | EEMSHVN  |
| Zeebrugge  | WIERMGDN     |          |



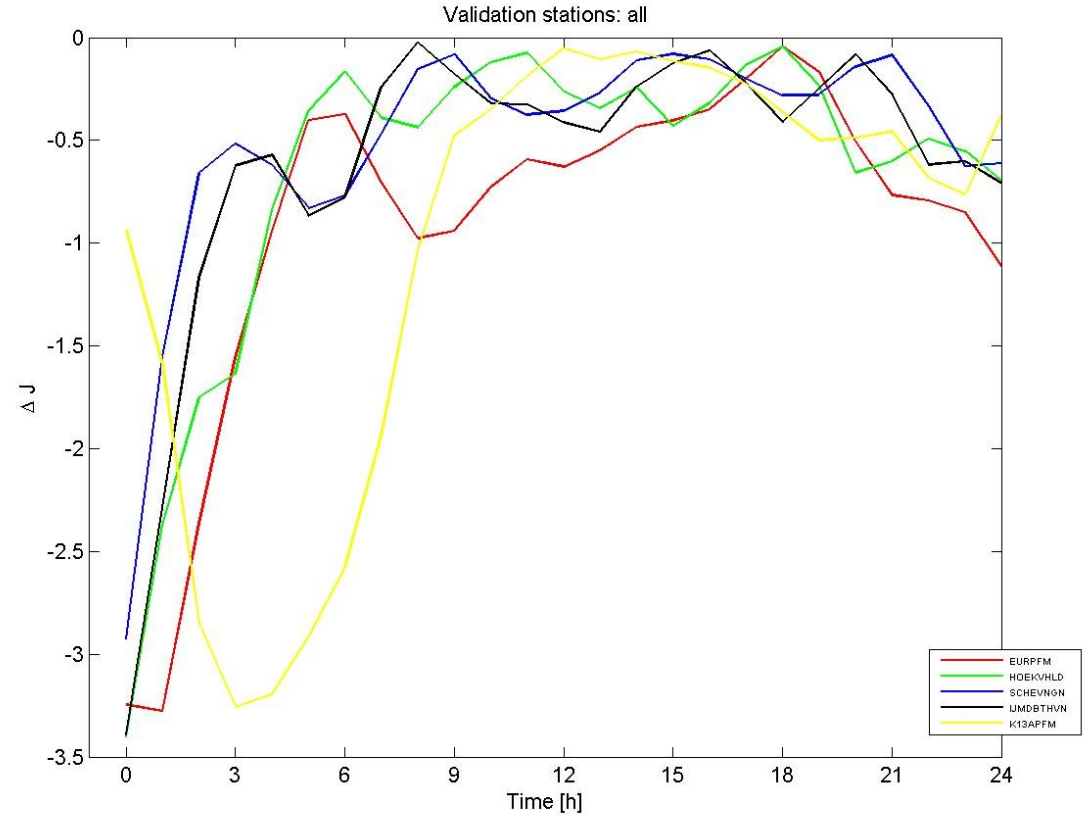
# Accuracy of DCSMv6 with Kalman filter



# Impact of assimilation stations

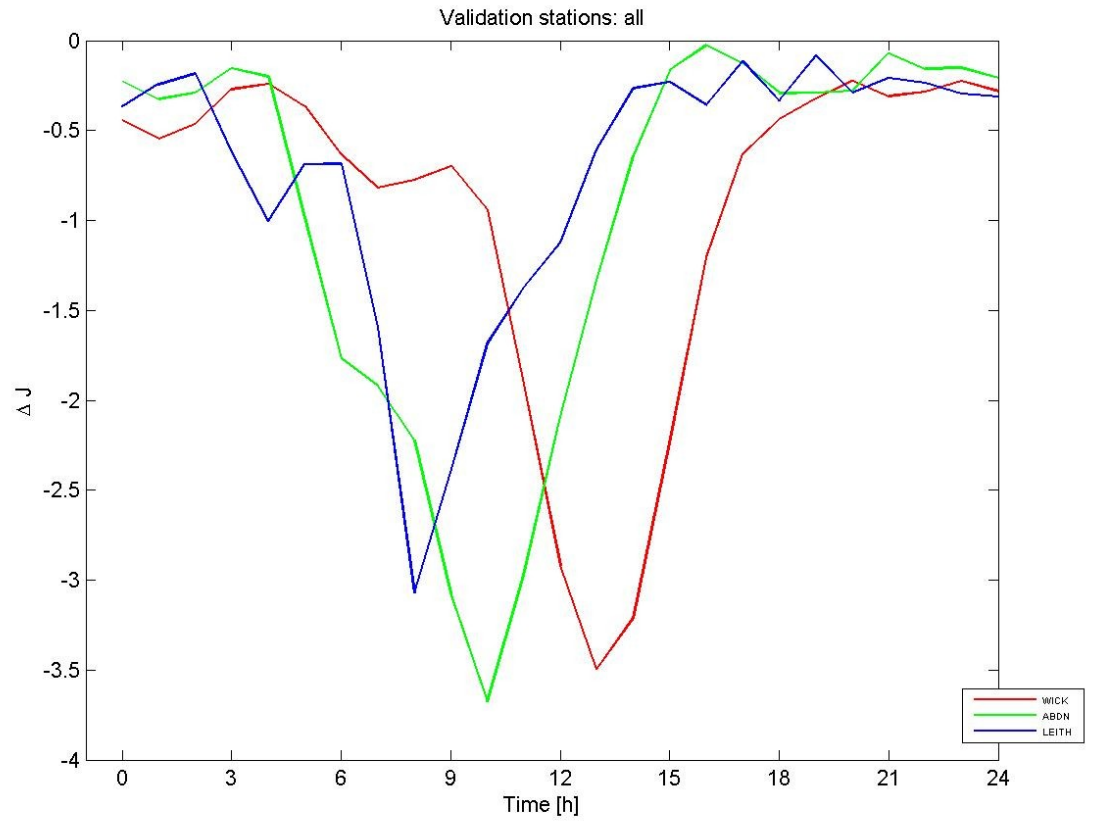
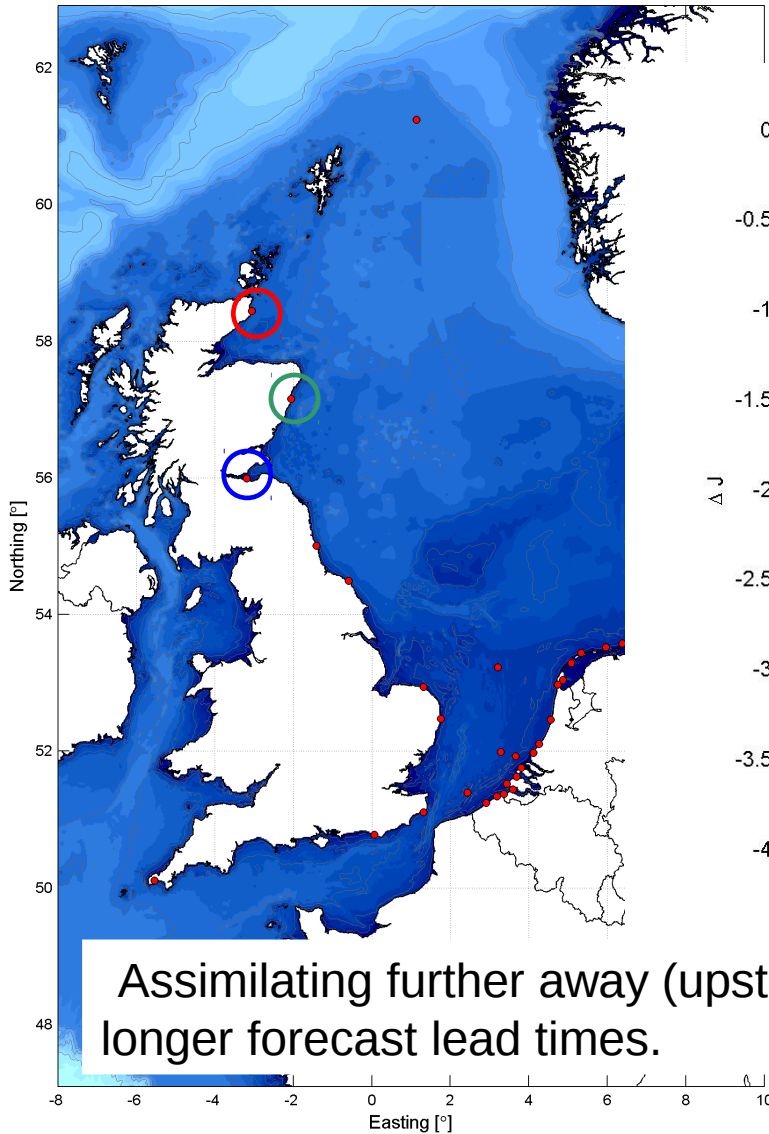
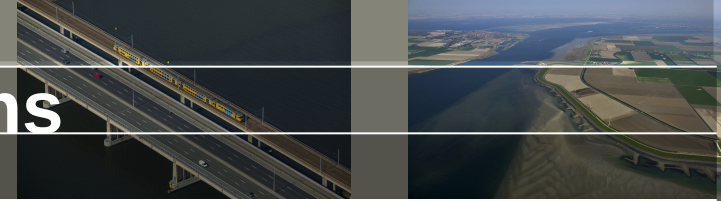


## J at coast Netherlands



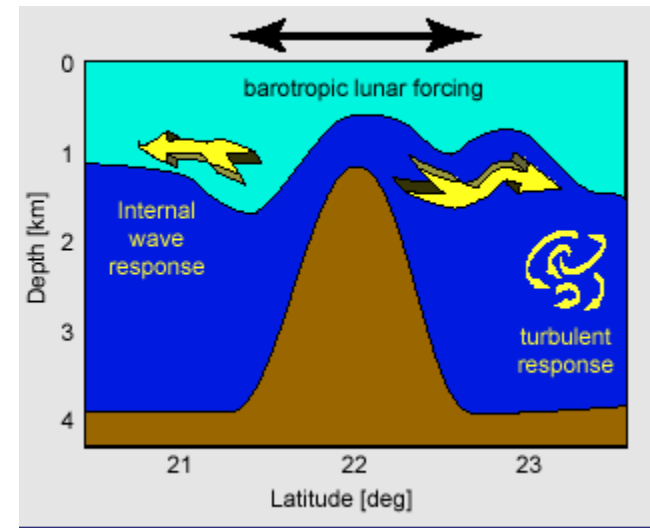
Assimilating nearby stations gives immediate impact on the forecast accuracy.

# Impact of assimilation stations



# Challenges and future work

- Dissipation by internal tides
- Self Attraction and Loading
- Open boundary





# Improved open boundaries & sensitivity



Image IBCAO  
Image U.S. Geological Survey  
Image Landsat  
Data SIO, NOAA, U.S. Navy, NGA, GEBCO

Google earth

**Deltares**



Questions?